

Vectors Answers

1)

<p>10 (i)</p> $\begin{pmatrix} 29 \\ -13 \end{pmatrix} - \begin{pmatrix} 5 \\ -6 \end{pmatrix} = \begin{pmatrix} 24 \\ -7 \end{pmatrix}$ <p>Magnitude = 25, unit vector $\frac{1}{25} \begin{pmatrix} 24 \\ -7 \end{pmatrix}$</p>	<p>M1</p>	<p>M1 for subtraction</p>
<p>(ii)</p> $2\overline{AC} = 3\overline{AB}$ <p>or $2\overline{AB} + 2\overline{BC} = 3\overline{AB}$ leading to</p> $\overline{AC} = \begin{pmatrix} 36 \\ -10.5 \end{pmatrix}$ $\overline{OC} = \overline{OA} + \overline{AC}$ <p>or $\overline{OB} - \overline{OA} = 2\overline{OC} - 2\overline{OB}$</p> <p>leading to $\overline{OC} = \begin{pmatrix} 41 \\ -16.5 \end{pmatrix}$</p> <p>(equivalent methods acceptable)</p>	<p>M1</p> <p>A1</p>	<p>M1 for attempt to find magnitude of their vector</p> <p>M1 for attempt to find \overline{AC} – may be part of a larger method</p> <p>M1 for attempt to find \overline{OC}</p> <p>A1 for each</p>
	<p>[7]</p>	

2)

<p>(i) $\overline{OM} = \overline{OP} + \overline{PM} = p + \frac{1}{2}\overline{PQ}$ [or $q + \frac{1}{2}\overline{QP}$] = $\frac{3}{2}p + \frac{1}{2}q$</p> <p>$\overline{OX} = m(\frac{3}{2}p + \frac{1}{2}q)$</p>	<p>M1</p> <p>A1</p>
<p>(ii) $\overline{PN} = \overline{ON} + \overline{PO} = \frac{2}{5}q - p \Rightarrow \overline{PX} = n(\frac{2}{5}q - p)$</p> <p>$\overline{OX} = p + n(\frac{2}{5}q - p)$</p>	<p>M1 A1</p> <p>A1√</p>
<p>(iii) Solve $1 - n = \frac{3}{2}m$ $\frac{2}{5}n = \frac{1}{2}m$</p> <p style="text-align: right;">$\Rightarrow \quad n = \frac{5}{9}$ $m = \frac{2}{3}$</p>	<p>M1 A1</p>

Vectors Answers

3)

<p>4 (i) Modulus of $(3\mathbf{i} - 4\mathbf{j})$ or $(4\mathbf{i} + 3\mathbf{j}) = 5$</p> <p>$\overrightarrow{OP} = (3\mathbf{i} - 4\mathbf{j}) \times (10+5) = 6\mathbf{i} - 8\mathbf{j}$</p> <p>$\overrightarrow{OQ} = (4\mathbf{i} + 3\mathbf{j}) \times (15+5) = 12\mathbf{i} + 9\mathbf{j}$</p> <p>(ii) $\overrightarrow{PQ} = 12\mathbf{i} + 9\mathbf{j} - (6\mathbf{i} - 8\mathbf{j}) = 6\mathbf{i} + 17\mathbf{j}$</p> <p>Magnitude = $\sqrt{6^2 + 17^2} = \sqrt{325} = 5\sqrt{13}$</p> <p style="text-align: center;">$\lambda = 5$</p>	<p>B1</p> <p>M1 A1</p> <p style="text-align: center;">[3]</p> <p>M1 M1</p> <p>A1</p> <p style="text-align: center;">[3]</p>	<p>Anywhere.</p> <p>Mult. by 10 (or 15) + modulus - once. Both correct.</p> <p>q-p or p-q Allow if p+q used.</p> <p>Allow if p-q used.</p>
---	---	---

4)

<p>(i) $\mathbf{a} = \frac{1}{13} (5\mathbf{i} - 12\mathbf{j})$</p>	<p>M1, A1</p> <p style="text-align: center;">[2]</p>	<p>M1 for a valid attempt to obtain magnitude.</p>
<p>(ii) $q(5\mathbf{i} - 12\mathbf{j}) + p\mathbf{i} + \mathbf{j} = 19\mathbf{i} - 23\mathbf{j}$</p> <p>$5q + p = 19$</p> <p>$-12q + 1 = -23$</p> <p>Leading to $q = 2, p = 9$</p>	<p>M1</p> <p>M1</p> <p>A1 [3]</p>	<p>M1 for equating like vectors</p> <p>M1 for solution of (simultaneous) equations</p> <p>A1 for both</p>

5)

(i)	$\sqrt{7^2 + 24^2}$	M1
	$ OA = 25$	A1
(ii)	$\overrightarrow{AB} = \begin{pmatrix} 3 \\ -4 \end{pmatrix}$	B1
	$ AB = 5$	B1
(iii)	$\overrightarrow{AC} = 5\overrightarrow{AB} = \begin{pmatrix} 15 \\ -20 \end{pmatrix}$	M1
	$\overrightarrow{OC} = \overrightarrow{OA} + \overrightarrow{AC}$	M1
	$\begin{pmatrix} 22 \\ 4 \end{pmatrix}$	A1

Vectors Answers

6)	(i)	$\overrightarrow{OP} = \frac{3}{5}\mathbf{a} + \frac{2}{5}\mathbf{b} \text{ oe}$ $\overrightarrow{OX} = \mu\left(\frac{3}{5}\mathbf{a} + \frac{2}{5}\mathbf{b}\right)$	M1 A1
			A1
	(ii)	$\overrightarrow{OX} = \mathbf{a} + \lambda\mathbf{b} \text{ or } \overrightarrow{AX} = \mu\left(\frac{3}{5}\mathbf{a} + \frac{2}{5}\mathbf{b}\right) - \mathbf{a}$ <p>Equates a components</p> $\mu = \frac{5}{3}$ <p>Equates b components</p> $\lambda = \frac{2}{3}$	B1
			M1
			A1
			M1
			A1
			[8]

7)	(i)	$\overrightarrow{AQ} = 3b - a$ $\overrightarrow{OX} = \overrightarrow{OA} + \mu\overrightarrow{AQ}$ $a + \mu(3b - a)$	
	(ii)	$\overrightarrow{BP} = 2a - b$ $\overrightarrow{OX} = \overrightarrow{OB} + \lambda\overrightarrow{BP}$ $b + \lambda(2a - b)$	
	(iii)	<p>Equate vectors and solve</p> $\begin{cases} 1 - \mu = 2\lambda \\ 3\mu = 1 - \lambda \end{cases}$ $\mu = 0.2$ $\lambda = 0.4$	

8)	(i)	$\overrightarrow{OX} = \mathbf{a} + \mu(\mathbf{b} - \mathbf{a}) \text{ or } (1 - \mu)\mathbf{a} + \mu\mathbf{b}$	M1A1
	(ii)	$\overrightarrow{OS} = \frac{3}{5}\mathbf{a}$ $\overrightarrow{OT} = \frac{7}{5}\mathbf{b}$ $\overrightarrow{OX} = \frac{3}{5}\mathbf{a} + \lambda\left(\frac{7}{5}\mathbf{b} - \frac{3}{5}\mathbf{a}\right) \text{ or } \overrightarrow{OX} = (1 - \lambda)\frac{3}{5}\mathbf{a} + \lambda\frac{7}{5}\mathbf{b}$	B1
			B1
	(iii)	<p>Equate components or arrange to $(\alpha)\mathbf{a} = (\beta)\mathbf{b}$ and put $\alpha = \beta = 0$</p> <p>Solve simultaneous equations</p> $\lambda = \frac{1}{2}$ $\mu = \frac{7}{10}$	M1A1
			M1
			DM1
			A1
			A1
			[10]

Vectors Answers

9)

(i)	$\overrightarrow{OP} = 3\mathbf{c}$	
	$\overrightarrow{OQ} = \frac{3}{2}\mathbf{d}$	B1
	$\overrightarrow{DR} = \overrightarrow{CD} = \mathbf{d} - \mathbf{c}$	B1
	$\overrightarrow{OR} = \overrightarrow{OD} + \overrightarrow{DR} = 2\mathbf{d} - \mathbf{c}$	M1A1
(ii)	Finds two of \overrightarrow{PQ} , \overrightarrow{QR} , \overrightarrow{PR}	M1
	Two of $\overrightarrow{PQ} = \frac{3}{2}\mathbf{d} - 3\mathbf{c}$, $\overrightarrow{QR} = \frac{1}{2}\mathbf{d} - \mathbf{c}$, $\overrightarrow{PR} = 2\mathbf{d} - 4\mathbf{c}$	A1+A1
	Express one vector as multiple of another	M1
	3:1	A1
		[10]