

Trig Functions and Identities 2 ANSWERS

1)

10	(i)	$\tan x = -1.33$ 126.9 306.9	B1 B1 B1√
	(ii)	$6 \cos y + \frac{6}{\cos y} = 13$ or $\frac{6}{\sec y} + 6 \sec y = 13$ Forms quadratic in $\cos y$ or $\sec y$ ($6\cos^2 y - 13\cos y + 6 = 0$) Solve 3 term quadratic 48.2 311.8	B1 M1 M1 A1 A1√
	(iii)	$2z - 3 = 0.775$ (or 2.37) radians Solves for z using radians 1.89 and 2.68	B1 M1 A1

[11]

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2)

4	(a)	Expresses with common denominator $\frac{2 \sin x}{\cos^2 x}$ $2 \frac{\sin x}{\cos x} \frac{1}{\cos x} = 2 \tan x \sec x$ or $2 \tan x \frac{1}{\cos x} = 2 \tan x \sec x$	M1 A1 A1 ag
	(b)	$\cos x = \sqrt{1-p^2}$ $\operatorname{cosec} 2x = \frac{1}{\sin 2x}$ $\frac{1}{2p\sqrt{1-p^2}}$	B1 B1 B1
			[6]

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3)

1	$\frac{1}{\frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta}}$	M1	M1 for adding fractions in terms of sin/cos/tan/cot correctly
	$= \frac{\sin \theta \cos \theta}{\sin^2 \theta + \cos^2 \theta}$	M1	M1 for use of correct identity
	$= \sin \theta \cos \theta$	A1	A1 for correct solution only
	OR	[3]	
	$\frac{\tan \theta}{\tan^2 \theta + 1}$ or $\frac{\cot \theta}{\cot^2 \theta + 1}$	M1	M1 for adding fractions in terms of tan/cot correctly
	$= \frac{\tan \theta}{\sec^2 \theta}$ or $\frac{\cot \theta}{\operatorname{cosec}^2 \theta}$	M1	M1 for use of correct identity
$= \sin \theta \cos \theta$	A1	A1 for correct solution only	

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4)

<p>2</p> $\sqrt{\frac{\sin^2 \theta}{4 \tan^2 \theta}}$ $= \frac{\sin \theta}{2 \tan \theta}$ $= \frac{\cos \theta}{2}, k = 0.5$ <p>OR</p> $\sqrt{\frac{1 - \cos^2 \theta}{4} - 4}$ $= \sqrt{\frac{1 - \cos^2 \theta}{4 - 4 \cos^2 \theta}}$ $= \frac{\cos \theta}{2}$	<p>B1 B1</p> <p>M1</p> <p>A1 [4]</p> <p>B1</p> <p>B1</p> <p>M1 A1</p>	<p>B1 for numerator B1 for denominator</p> <p>M1 for rearrangement</p>
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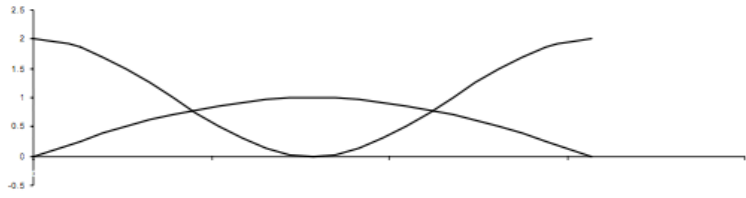
5)

<p>7 (a)</p> $\cot^2 x = \frac{1}{\tan^2 x}$ $\operatorname{cosec}^2 x = 1 + \cot^2 x$ $= 1 + \frac{1}{p^2} \text{ or } \frac{p^2 + 1}{p^2}$ <p>OR Draw triangle with 1, p and $p^2 + 1$ correct B1</p> $\operatorname{cosec} x = \frac{\sqrt{p^2 + 1}}{p} \text{ B1} \quad \operatorname{cosec}^2 x = \frac{p^2 + 1}{p^2} \text{ B1}$ <p>(b)</p> $\sec \theta = \frac{1}{\cos \theta}$ <p>Multiply out and correct use Pythagoras</p> $\frac{\sin^2 \theta}{\cos \theta} = \sin \theta \tan \theta$	<p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p>	<p>[7]</p>
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6)

<p>2 (i)</p>  <p>Sine curve through (0, 0), (90, 1), (180, 0)</p> <p>Cosine curve through (0, 2), (45, 1), (90, 0), (135, 1), (180, 2)</p> <p>(ii) 2</p> <p>(iii) $2\sqrt{\quad}$</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>B1√</p> <p>B1√</p> <p>[5]</p>
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7)

<p>11 (i) $\tan \frac{1}{2}x = 4$</p> <p>$\left(\frac{1}{2}x = \right) 76$</p> <p>151.9 or 152</p> <p>(ii) $\tan y \cos y = \sin y$ and $\cos^2 y = 1 - \sin^2 y$</p> <p>Solve quadratic</p> <p>$\sin y = 0 \Rightarrow y = 180$</p> <p>36.9</p> <p>143(.1)</p> <p>(iii) $\cos z = \pm \frac{\sqrt{3}}{2}$ or $\tan z = \pm \frac{1}{\sqrt{3}}$ or $\sin z = \pm \frac{1}{2}$</p> <p>$\frac{\pi}{6}$ and $\frac{11\pi}{6}$ or $\frac{\pi}{6}$ and $\frac{7\pi}{6}$ or $\frac{\pi}{6}$ and $\frac{5\pi}{6}$</p> <p>$\frac{5\pi}{6}$ and $\frac{7\pi}{6}$ or $\frac{5\pi}{6}$ and $\frac{11\pi}{6}$ or $\frac{7\pi}{6}$ and $\frac{11\pi}{6}$</p>	<p>B1</p> <p>B1</p> <p>B1√</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>A1√</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>[11]</p>
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8)

<p>2 (i) Graphs</p>	<p>B1</p> <p>B1</p> <p>[2]</p>	<p>B1 for one correct curve</p> <p>B1 for a second correct curve consistent with the first curve</p>
<p>(ii) 3</p>	<p>√ B1</p> <p>[1]</p>	<p>Follow through on number of clear points of intersection</p>

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9)

3	$\frac{\cos x(1 + \sin x) + \cos x(1 - \sin x)}{1 - \sin^2 x}$ $\frac{2 \cos x}{\cos^2 x}$ $2 \sec x$	<p>M1</p> <p>DM1</p> <p>M1</p> <p>A1</p> <p>[4]</p>	<p>M1 for attempt to get in terms of a single fraction</p> <p>DM1 simplifying numerator</p> <p>M1 simplifying denominator</p>
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