

Remainder / Factor Theorem 2

- 1) The expression  $6x^3 + ax^2 - (a + 1)x + b$  has a remainder of 15 when divided by  $x + 2$  and a remainder of 24 when divided by  $x + 1$ . Show that  $a = 8$  and find the value of  $b$ . [5]
- 2) The expression  $x^3 + ax^2 - 15x + b$  has a factor  $x - 2$  and leaves a remainder of 75 when divided by  $x + 3$ . Find the value of  $a$  and of  $b$ . [5]
- 3) Solve the equation  $3x^3 + 7x^2 - 22x - 8 = 0$ . [6]
- 4) The remainder when the expression  $x^3 + kx^2 - 5x - 3$  is divided by  $x - 2$  is 5 times the remainder when the expression is divided by  $x + 1$ . Find the value of  $k$ . [4]
- 5) Factorise completely the expression  $2x^3 - 11x^2 - 20x - 7$ . [5]
- 6) Solve the equation  $2x^3 - 3x^2 - 11x + 6 = 0$ . [6]
- 7) (i) Show that  $2x - 1$  is a factor of  $2x^3 - 5x^2 + 10x - 4$ . [2]  
  
(ii) Hence show that  $2x^3 - 5x^2 + 10x - 4 = 0$  has only one real root and state the value of this root. [4]
- 8) The expression  $x^3 + 8x^2 + px - 25$  leaves a remainder of  $R$  when divided by  $x - 1$  and a remainder of  $-R$  when divided by  $x + 2$ .  
  
(i) Find the value of  $p$ . [4]  
  
(ii) Hence find the remainder when the expression is divided by  $x + 3$ . [2]