

Remainder / Factor Theorem 2 Answers

1)

<p>2 $6(-2)^3 + a(-2)^2 - (a+1)(-2) + b = 15$ $6a + b = 61$ when $x = -1$, $2a + b = 29$</p> <p>leading to $a = 8$ and $b = 13$</p>	<p>M1 A1 A1 M1 A1</p>	<p>M1 for substitution of $x = -2$ or -1, or verification A1 for each correct (allow unsimplified)</p> <p>M1 for attempt to solve A1 for $a = 8, b = 13$</p>
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2)

<p>2 Find $f(2)$ or $f(-3)$ or long division to remainder $8 + 4a - 30 + b = 0$ or $4a + b = 22$ $-27 + 9a + 45 + b = 75$ or $9a + b = 57$</p> <p>Solve simultaneous equations $a = 7, b = -6$</p>	<p>M1 A1 A1</p> <p>M1 A1</p>
[5]	

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3)

<p>6 $x = 2$ or -4 or $-\frac{1}{3}$</p> <p>Either $(x-2)(3x^2 + 13x + 4)$ or $(x+4)(3x^2 - 5x - 2)$ or $(3x+1)(x^2 + 2x - 8)$ $(x-2)(x+4)(3x+1)$</p> <p>$x = 2, -4, -\frac{1}{3}$</p>	<p>B1 M1 A1 M1, A1 A1</p>	<p>B1 for spotting a solution M1 for attempt to get quadratic factor A1 for correct quadratic factor M1 for dealing with quadratic factor A1 for correct factors A1 for all solutions</p>
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4)

<p>4 $f(2) = 8 + 4k - 10 - 3$ $f(-1) = -1 + k + 5 - 3$ $(4k - 5) = 5(k + 1)$ leading to $k = -10$</p>	<p>M1 M1 M1 A1</p>	<p>M1 for use of $x = 2$ M1 for use of $x = -1$ M1 for attempt to link the two remainders</p>
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5)

<p>4 $x = -1$ or 7 or $-\frac{1}{2}$ seen</p> <p>Either $(x+1)(2x^2 - 13x - 7)$ or $(x-7)(2x^2 + 3x + 1)$ or $(2x+1)(x^2 - 6x - 7)$ leading to $(x+1)(x-7)(2x+1)$</p>	<p>M1 DM1 A1 DM1, A1</p>	<p>M1 for attempt to find a root DM1 for attempt to obtain quadratic factor A1 correct quadratic factor DM1 attempt to factorise quadratic factor</p>
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6)

5 Search for first root or factor

M1

$$x = -2 \text{ or } \frac{1}{2} \text{ or } 3 \text{ or } (x + 2) \text{ or } (x - 3) \text{ or } (2x - 1)$$

A1

Attempt to factorise cubic

M1

$$(x + 2)(2x^2 - 7x + 3)$$

$$\text{or } (x - 3)(2x^2 + 3x - 2)$$

A1

$$\text{or } (2x - 1)(x^2 - x - 6)$$

Solve 3 term quadratic

M1

$$x = -2 \text{ and } \frac{1}{2} \text{ and } 3$$

A1 [6]

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7)

$$\begin{aligned} \mathbf{5} \quad \mathbf{(i)} \quad & 2\left(\frac{1}{8}\right) - 5\left(\frac{1}{4}\right) + 10\left(\frac{1}{2}\right) - 4 \\ & = 0 \end{aligned}$$

M1

M1 for substitution of $x = 0.5$ or attempt at long division

A1

$$\mathbf{(ii)} \quad (2x - 1)(x^2 - 2x + 4)$$

M1A1

M1 attempt to obtain quadratic factor

$$\text{For } (x^2 - 2x + 4), 'b^2 < 4ac'$$

M1

A1 for correct quadratic factor
M1 for correct use of discriminant or solution of quadratic equation = 0

so only one real root of $x = 0.5$

A1

A1, all correct with statement of root.

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8)

5 (i)	$f(1) = 1 + 8 + p - 25 (= p - 16)$	B1	
	$f(-2) = -8 + 32 - 2p - 25 (= -2p - 1)$	B1	
	$p - 16 = 2p + 1$ oe	M1	
	$p = -17$	A1	
(ii)	Evaluates $f(-3)$ or divides by $(x + 3)$ to remainder	M1	
	$71 (= 20 - 3p)$	A1√	

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