Quadratic Expressions and Equations

| 1) | 1 | (i) | a = -12, b = -4 | B1, B1 [2] | B1 for each |
|----|---|------|-----------------|------------|---------------------------------|
| | | (ii) | -4 | √B1 [1] | Follow through on their y value |

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| 2) | | | |
|----|---|---|-----------------|
| | 5 | Eliminate y $x^2 + (8 - m)x + 9 = 0$ | M1 A1 |
| | | Use $b^2 * 4ac$ Reach $(8-m) * \pm 6$ or solves $m^2 - 16m + 28 * 0$ (* is either > or =) | DM1 DDM1 |
| | | m = 2 and 14 $m < 2$, $m > 14$ | A1 A1 [6] |

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| 3) | 3 $4(2k+1)^2 = 4(k+2)$ $4k^2 + 3k - 1 = 0$ leading to $k = \frac{1}{4}, -1$ | M1 A1 M1 A1 [4] | M1 for use of ' $b^2 - 4ac$ ' Correct quadratic equation M1 for correct attempt at solution A1 for both 1 values | |
|----|---|-----------------------------|---|-----|
| | _ | 2 2 4 | | i i |

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| 4) | 7 (i) $y = 4x^2 - 12x + 3$ $y = (2x - 3)^2 - 6$ | B1 B1 B1 | [3] | B1 for 2 (part of linear factor) B1 for -3 (part of linear factor) B1 for -6 |
|----|--|----------------|-----|--|
| | (ii) $\left(\frac{3}{2},-6\right)$ | √B1, √B1 | [2] | Follow through on their a , b and c Allow calculus method. |
| | (iii) f≥-6 | √B1 | [1] | Follow through on their c |

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| 5) | 1 | $x^{2} + (2k+10)x + (k^{2}+5) = 0$ | M1 | | M1 for equating to zero and use of |
|----|---|--|------------|-----|---|
| | | ` | | | $b^2 = 4ac$ |
| | | $(2k+10)^2 = 4(k^2+5)$ | M1 | | M1 for solution |
| | | k = -2 | A1 | | |
| | | dv | | [3] | |
| | | (or $\frac{dy}{dx} = 2x + (2k+10), x = -(k+5)$ | M1 | | M1 for differentiation and attempt to equate to zero. |
| | | $0 = (k+5)^{2} - (2k+10)(k+5) + k^{2} + 5$ | M1 | | $\hat{M1}$ for attempt to substitute in for x in |
| | | leading to $k = -2$) | A1 | | terms of k , for $y = 0$ and for attempt at solution. |
| | | $(\text{or } (x+A)^2 = x^2 + (2k+10)x + k^2 + 5$ | M1 | | M1 for approach |
| | | $A = (k+5), A^2 = k^2 + 5$ | M1 | | M1 for equating and attempt at solution |
| | | $(k+5)^2 = k^2 + 5$, leading to $k = -2$) | A 1 | | |
| | | (or by completing the square | | | |
| | | $y = (x+(k+5))^2 - (k+5)^2 + (k^2+5)$ | M1 | | M1 for approach |
| | | $\left(k+5\right)^2 = k^2 + 5$ | M1 | | M1 for equating last 2 terms to zero and |
| | | leading to $k = -2$) | A 1 | | attempt to solve |
| | I | | l | | I I |

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| • | | 10 | 411 | [~] | |
|----|-------|------------------------------------|-----|--------|--|
| 6) | 4 | Eliminates y | M1 | | |
| | | $x^2 + kx - 2x + 16 (= 0)$ | A1 | | |
| | | Uses $b^2 - 4ac$ | M1 | | |
| | | $k^2 - 4k - 60*0$ or $(k-2)*\pm 8$ | A1 | | |
| | | k = -6 or 10 | A1 | | |
| | | k < -6 or k > 10 | A1 | [6] | |
| | - (*) | 61) 1 · 0 · 05 / 16) | D.1 | \neg | |

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| 7) | | | | |
|----|---|--|--------------|--|
| 7) | 1 | $24x^2 - 6x = 0$ | M1 | M1 for attempt to get an equation in one variable. |
| | | $(or y^2 + 3y + 2 = 0)$ | M1 | M1 for attempt to get 2 or 3 term quadratic = 0 |
| | | leading to (0, 1) and $\left(\frac{1}{4}, -2\right)$ | DM1 A1,A1 | DM1 for attempt to solve A1 for each pair of values |
| | | | [5] | |

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| 8) | | | | 1 |
|----|-------|--|------------|--|
| -, | 4 (i) | $5x - 3 = kx^2 - 3x + 5$ | M1 | M1 for equating line and curve equations |
| | | $kx^2 - 8x + 8 = 0$ | DM1, A1 | DM1 for use of $b^2 - 4ac$ on resulting |
| | | using $b^2 - 4ac = 0$, $k = 2$ | [3] | quadratic |
| | | (Alt scheme: $5 = 2kx - 3$, $x = \frac{4}{k}$ $\frac{20}{k} - 3 = \frac{16}{k} - \frac{12}{k} + 5$ | | (Alt scheme: M1 for attempt to differentiate quadratic and equate to 5 DM1 for simplification and solution using |
| | | k k k leading to $k = 2$) | | resulting quadratic |
| | (ii) | leading to $x = 2$, $y = 7$ | M1, A1 [2] | M1 for obtaining x and y coords |

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9)
3 Eliminates
$$x$$
 or y

$$7x^2 - 14x - 21 = 0 \text{ or } 7y^2 + 14y - 105 = 0 \text{ oe}$$
Solve 3 term quadratic
$$(x+1)(x-3)$$

$$(3,3) \text{ and } (-1,-5)$$
A1

[or $x = \frac{2 \pm \sqrt{16}}{2}$

$$-1 \text{ and } 3$$

$$(3,3) \text{ and } (-1,-5)$$
M1

A1

A1

A1

[5]

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