

Quadratic Expressions and Equations

- 1) The equation of a curve is given by  $y = 2x^2 + ax + 14$ , where  $a$  is a constant.  
Given that this equation can also be written as  $y = 2(x - 3)^2 + b$ , where  $b$  is a constant, find
- (i) the value of  $a$  and of  $b$ , [2]
  - (ii) the minimum value of  $y$ . [1]
- 2) Find the set of values of  $m$  for which the line  $y = mx - 2$  cuts the curve  $y = x^2 + 8x + 7$  in two distinct points. [6]
- 3) Find the values of  $k$  for which the equation  $x^2 - 2(2k + 1)x + (k + 2) = 0$  has two equal roots. [4]
- 4) (i) Express  $4x^2 - 12x + 3$  in the form  $(ax + b)^2 + c$ , where  $a, b$  and  $c$  are constants and  $a > 0$ . [3]  
(ii) Hence, or otherwise, find the coordinates of the stationary point of the curve  $y = 4x^2 - 12x + 3$ . [2]  
(iii) Given that  $f(x) = 4x^2 - 12x + 3$ , write down the range of  $f$ . [1]
- 5) Find the value of  $k$  for which the  $x$ -axis is a tangent to the curve
- $$y = x^2 + (2k + 10)x + k^2 + 5. \quad [3]$$
- 6) Find the set of values of  $k$  for which the line  $y = 2x - 5$  cuts the curve  $y = x^2 + kx + 11$  in two distinct points. [6]
- 7) Find the coordinates of the points of intersection of the curve  $y^2 + y = 10x - 8x^2$  and the straight line  $y + 4x + 1 = 0$ . [5]
- 8) The line  $y = 5x - 3$  is a tangent to the curve  $y = kx^2 - 3x + 5$  at the point  $A$ . Find
- (i) the value of  $k$ , [3]
  - (ii) the coordinates of  $A$ . [2]

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- 9) Find the coordinates of the points where the straight line  $y = 2x - 3$  intersects the curve  $x^2 + y^2 + xy + x = 30$ .

[5]