IB Questionbank Mathematical Studies 3rd edition

Prob with conditional MS

0 min 0 marks

1. (a)
$$-4, -3, -2, -1, 0, 1, 2$$
 (A1) (C1)
Note: Award (A1) for correct numbers do not penalise if

Note: Award (A1) for correct numbers, do not penalise if braces, brackets or parentheses seen.

(b)
$$\frac{4}{7}$$
 (0.571, 57.1%) (A1)(ft)(A1)(ft) (C2)

Notes: Award (A1)(ft) for numerator, (A1)(ft) for denominator. Follow through from part (a). *Note:* There is no further penalty in parts (c) and (d) for use of denominator consistent with that in part (b).

(c)
$$\frac{1}{7}$$
 (0.143, 14.3%) (A1)(ft) (C1)

Note: Follow through from part (a).

(d) $\frac{1}{7}$ (0.143, 14.3%) (A1)(ft)(A1)(ft) (C2)

Note: Award (A1)(*ft*) for numerator, (A1)(*ft*) for denominator. Follow through from part (a).

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2. (a)



Note: Award (A2) for 3 correctly placed values, and no extras (4 need not be seen), (A1) for 2 correctly placed values, (A0) for 1 or no correctly placed values.

(b)
$$18 + 10 + 6 - 30$$
 (M1)
= 4 (A1) (C2)

(c)
$$P(A \mid B) = \frac{4}{10} \left(\frac{2}{5}, 0.4, 40\%\right)$$
 (A1)(ft)(A1) (C2)

Note: Award (A1)(*ft*) for their numerator from part (b), (A1) for denominator.

3. (a) (i)
$$m = 1$$
 (A1)

(ii) n = 3 (A1) (C2) **Note:** Award (A0)(A1)(ft) for $m = \frac{1}{8}$, $n = \frac{3}{8}$ Award (A0)(A1)(ft) for m = 3, n = 1.

(b)
$$P(B/R') = \frac{\frac{3}{8}}{\frac{6}{8}} = \frac{3}{6} \left(\frac{1}{2}, 50\%, 0.5\right)$$
 (M1)(A1)(ft) (C2)

Note: Award (M1) for correctly substituted conditional probability formula or for 6 seen as part of denominator.

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(c)
$$P(B, B) = \frac{3}{8} \times \frac{3}{8} = \frac{9}{64}$$
 (0.141) (M1)(A1)(ft) (C2)

Note: Award (M1) for product of two correct fractions, decimals or percentages. (ft) from their answer to part (a) (ii).

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4. (a)
$$0.8 = 0.5 + 0.6 - P(A \cap B)$$
 (M1)
 $P(A \cap B) = 0.3$ (A1) (C2)
Note: Award (M1) for correct substitution, (A1) for correct

(b)
$$P(A \mid B) = \frac{0.3}{0.6}$$
 (M1)
= 0.5 (A1)(ft) (C2)

Note: Award (M1) for correct substitution in conditional probability formula. Follow through from their answer to part (a), provided probability is not greater than one.

(c)
$$P(A \cap B) = P(A) \times P(B)$$
 or $0.3 = 0.5 \times 0.6$ (R1)

OR

 $P(A \mid B) = P(A) \tag{R1}$

they are independent. (Yes) (A1)(ft) (C2) *Note:* Follow through from their answers to parts (a) or (b). Do not award (R0)(A1).

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5. (a)



answer.

(A1)(A1)(A1) (C3)

Note: Award (A1) for a labeled Venn diagram with appropriate sets. (A1) for 7, (A1) for 8 and 5. (b) P (Spanish / one language only) = $\frac{\frac{8}{20}}{\frac{8}{20} + \frac{5}{20}}$ (M1)(A1)(ft)

Note: Award (M1) for substituted conditional probability formula, (A1) for correct substitution. Follow through from their Venn diagram.

$$=\frac{8}{13} (0.615, 61.5\%)$$
(A1)(ft)

OR

P (Spanish / one language only) =
$$\frac{8}{8+5}$$
 (A1)(ft)(M1)

Note: Award (A1) for their correct numerator, (M1) for correct recognition of regions. *Follow through from their Venn diagram.*

$$=\frac{8}{13} (0.615, 61.5\%)$$
(A1)(ft) (C3)

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6. (a)
$$a = 4, b = 1$$
 (A1)(A1) 2

(b)
$$30 - (4 + 12 + 1 + 2 + 4 + 4) = 3$$
 (M1)(A1) (or (A2)) 2

(c)
$$\frac{24}{30} \left(=\frac{4}{5}\right)$$
 (A1)(A1) 2

Note: Award (A1) for numerator, (A1) for denominator.

(d)
$$\frac{6}{19}$$
 (A1)(A1) 2

Note: Award (A1) for numerator, (A1) for denominator.

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- (a) 3 intersecting circles and rectangle. (A1) correct numbers (A4) for all 7 numbers correct, (A3) for 6 correct, (A2) for 5 correct, (A1) for 4 correct. (Do not count the number in D only on the Venn Diagram at this stage.)
- (b) 4+5+3+4+2+2+15+x=40 (M1) 35+x=40 x=5Therefore, five play drums only. (A1) 2 (AG)

(c)
$$\frac{4}{40} \left(\frac{1}{10}, 10\%, 0.1 \right)$$
 (A2) 2

Note: Award (A1) for 4, (A1) for 40.

(d)
$$\frac{21}{40}(52.5\%, 0.525)$$
 (A2) 2

Note: Award (A1) for 21, (A1) for 40.

(e)
$$\frac{8}{16} \left(\frac{1}{2}, 50\%, 0.5 \right)$$
 (A3) 3

Note: Award (A1) for 8, (A2) for 16. Do not separate (A2).

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