

Module 2 Circle Theorems Answers

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6)

(a) 66°	2	M1 for 90° clearly identified as A
(b) 33°	1	
(c) 123°	2	B1 for OBA or $OAB = 57^\circ$

7

(a) 72	1	
(b) 36	1	
(c) 54	2ft	ft $90 - (b)$ M1 $POQ = 108$

8)

(a) 35	1	
(b) 55	1ft	$90 - (a)$ but $b > 0$
(c) 55	1ft	$= (b)$
(d) 125	1ft	$180 - (c)$