

1)c Solve the equation  $\log_{27} x = 1 - \log_{27} (x - 0.4)$ .

2)c Given that  $\log_5 x = y$ , express each of the following in terms of  $y$ .

(a)  $\log_5 x^2$

(b)  $\log_5 \left( \frac{1}{x} \right)$

(c)  $\log_{25} x$

3)c Let  $p = \log_{10} x$ ,  $q = \log_{10} y$  and  $r = \log_{10} z$ .

Write the expression  $\log_{10} \left( \frac{x}{y^2 \sqrt{z}} \right)$  in terms of  $p$ ,  $q$  and  $r$ .

4)c Write each of the following in its simplest form

(a)  $e^{\ln x}$ ;

(b)  $e^{(\ln x + \ln y)}$ ;

(c)  $\ln(e^{x+y})^2$ .

5)c Let  $a = \log x$ ,  $b = \log y$ , and  $c = \log z$ .

Write  $\log \left( \frac{x^2 \sqrt{y}}{z^3} \right)$  in terms of  $a$ ,  $b$  and  $c$ .

6)c (a) Given that  $\log_3 x - \log_3 (x - 5) = \log_3 A$ , express  $A$  in terms of  $x$ .

(b) Hence or otherwise, solve the equation  $\log_3 x - \log_3 (x - 5) = 1$ .

7)c (a) Let  $\log_c 3 = p$  and  $\log_c 5 = q$ . Find an expression in terms of  $p$  and  $q$  for

(i)  $\log_c 15$ ;

(ii)  $\log_c 25$ .

(b) Find the value of  $d$  if  $\log_d 6 = \frac{1}{2}$ .