# IGCSE - Histograms 

49 min
43 marks

1. The speeds ( $v$ kilometres/hour) of 150 cars passing a $50 \mathrm{~km} / \mathrm{h}$ speed limit sign are recorded. A cumulative frequency curve to show the results is drawn below.

(a) Use the graph to find
(i) the median speed,
(ii) the inter-quartile range of the speeds,
(iii) the number of cars travelling with speeds of more than $50 \mathrm{~km} / \mathrm{h}$.
(b) A frequency table showing the speeds of the cars is

| Speed $(v \mathrm{~km} / \mathrm{h})$ | $30<v \leq$ <br> 35 | $35<v \leq 40$ | $40<v \leq 45$ | $45<v \leq 50$ | $50<v \leq 55$ | $55<v \leq 60$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 10 | 17 | 33 | 42 | $n$ | 16 |

(i) Find the value of $n$
(ii) Calculate an estimate of the mean speed.

## Answer the whole of this question on a sheet of graph paper.

(c) Another frequency table for the same speeds is

| Speed $(v \mathrm{~km} / \mathrm{h})$ | $30<v \leq 40$ | $40<v \leq 55$ | $55<v \leq 60$ |
| :---: | :---: | :---: | :---: |
| Frequency | 27 | 107 | 16 |

Draw an accurate histogram to show this information.
Use 2 cm to represent 5 units on the speed axis and 1 cm to represent 1 unit on the frequency density axis (so that $1 \mathrm{~cm}^{2}$ represents 2.5 cars).
2. (a) 100 students are given a question to answer.

The time taken ( $t$ seconds) by each student is recorded and the results are shown in the table.

| $t$ | $0<t \leq 20$ | $20<t \leq 30$ | $30<t \leq 35$ | $35<t \leq 40$ | $40<t \leq 50$ | $50<t \leq 60$ | $60<t \leq 80$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 10 | 10 | 15 | 28 | 22 | 7 | 8 |

(i) Calculate an estimate of the mean time taken.
(ii) Two students are picked at random.

What is the probability that they both took more than 50 seconds?
Give your answer as a fraction in its lowest terms.

## Answer part (b) on a sheet of graph paper.

(b) The data in part (a) is re-grouped to give the following table.

| $t$ | $0<t \leq 30$ | $30<t \leq 60$ | $60<t \leq 80$ |
| :---: | :---: | :---: | :---: |
| Frequency | $p$ | $q$ | 8 |

(i) Write down the values of $p$ and $q$.
(ii) Draw an accurate histogram to show these results.

Use a scale of 1 cm to represent 5 seconds on the horizontal time axis.
Use a scale of 1 cm to 0.2 units of frequency density (so that $1 \mathrm{~cm}^{2}$ on your histogram represents 1 student).
3. A group of students takes an English test.

The results are shown in the histogram.

Frequency density


100 students score marks in the range $50<x \leq 75$.
(i) How many students score marks in the range $0<x \leq 50$ ?
(ii) How many students score marks in the range $75<x \leq 100$ ?
(iii) Calculate an estimate of the mean mark of this group of students.
4. The mass, $m$ grams, of each of 200 chocolates is noted and the results are shown in the table.

| Mass ( $m$ grams) | $10<m \leq 20$ | $20<m \leq 22$ | $22<m \leq 24$ | $24<m \leq 30$ |
| :---: | :---: | :---: | :---: | :---: |
| Frequency | 35 | 115 | 26 | 24 |

(i) Calculate an estimate of the mean mass of a chocolate.
(ii) On a histogram, the height of the column for the $20<m \leq 22$ interval is 11.5 cm .

Calculate the heights of the other three columns.
Do not draw the histogram.

