A: Manipulate Expressions (I)

1) Factorise $3 x+12$ $3(x+4)$
2) Factorise fully

$$
2 x^{2}-4 x y
$$

$$
2 x(x-2 y)
$$

3) Expand and simplify $3(2 a+5)+5(a-2)$

$$
6 a+15+5 a-10=11 a+5
$$

4) Expand

$$
x(x+2)
$$

$$
x^{2}+2 x
$$

5) Factorise

$$
\begin{aligned}
& 15 x-10 \\
& 5(3 x-2)
\end{aligned}
$$

6) Expand and simplify $2(x-y)-3(x-2 y)$

$$
\begin{aligned}
& 2 x-2 y-3 x+6 y=-x+4 y \\
& \text { implify } \quad x^{5} \times x^{4}
\end{aligned}
$$

7) Simplify
$x^{9}$
8) Simplify

$$
x^{7} \div x^{2}
$$

$$
x^{6}
$$

9) Expand and simplify $3(2 a+5)+5(a-2)$ $6 a+15+5 a-10=11 a+5$
10) Expand and simplify $(x+5)(x+7)$
$x^{2}+5 x+7 x+35=x^{2}+12 x+35$

B: Manipulate Expressions (II)

1) Factorise

$$
\begin{gathered}
p^{2}-6 p+5 \\
(p-5)(p-1)
\end{gathered}
$$

2) Expand and simplify $(p+9)(p-4)$

$$
\begin{array}{cc}
p^{2}+9 p-4 p-36=p^{2}+5 p-36 \\
\text { actorise } & x^{2}-11 x+18
\end{array}
$$

3) Factorise

$$
(x-9)(x-2)
$$

4) Factorise

$$
x^{2}-49
$$

$$
(x+7)(x-7)
$$

5) Simplify

$$
\begin{aligned}
& \left(9 x^{8} y^{3}\right)^{\frac{1}{2}} \\
& x^{4} y^{3 / 2}
\end{aligned}
$$

6) Factorise

$$
\begin{gathered}
8 x-20 \\
4(2 x-5)
\end{gathered}
$$

7) Factorise
8) Factorise

$$
10 x^{2}-15 x y
$$

$$
5 x(2 x-3 y)
$$

$$
(x+8)(x-8)
$$

9) Expand and simplify $(x+7)(x-5)$

$$
x^{2}+7 x-5 x-35=x^{2}+2 x-35
$$

C: Manipulate Expressions (III)

1) Expand and simplify $(t+5)(t-4)$

$$
t^{2}+5 t-4 t-20=t^{2}+t-20
$$

2) Factorise

$$
x^{2}+17 x+60
$$

$$
(x+12)(x+5)
$$

3) Factorise $x^{2}-144$

$$
(x+12)(x-12)
$$

4) Factorise

$$
(2 x+3)(x-5)^{2 x^{2}-7 x-15}
$$

5) Simplify
$5 x^{4} y^{3} \times x^{2} y$
$5 x^{6} y^{4}$
6) Simplify

$$
\frac{45 e^{6} f^{8}}{5 e f^{2}} \quad 9 e^{5} f^{6}
$$

7) Factorise
$4 x^{2}-1$

$$
(2 x+1)(2 x-1)
$$

8) Factorise
$2 x^{2}+3 x+1$
$(2 x+1)(x+1)$
9) Simplify
$\left(m^{3}\right)^{5}$
$m^{15}$

## D: Surds

1) Rationalise the denominator
2) Expand and simplify
$(3-\sqrt{2})(3+\sqrt{2})$
$9+3 \sqrt{2}-3 \sqrt{2}-2=7$
3) Express $\frac{6}{\sqrt{2}}$ in the form $a \sqrt{b}$

$$
\frac{6 \sqrt{2}}{2}=3 \sqrt{2}
$$

4) Expand and simplify $(2+\sqrt{3})(1+\sqrt{3})$
$2+2 \sqrt{3}+\sqrt{3}+3=5+3 \sqrt{3}$
5) Rationalise the denominator
6) Expand and simplify
$(2+\sqrt{3})(7-\sqrt{3})$
$14-2 \sqrt{3}+7 \sqrt{3}-3=11+5 \sqrt{3}$
7) Rationalise the denominator $\frac{1}{\sqrt{3}}$
8) Express $\frac{\sqrt{18}+10}{\sqrt{2}}$ in the form $p+q \sqrt{2}$
$\frac{\sqrt{2}(\sqrt{18}+10)^{2}}{2}=\sqrt{56+10 \sqrt{2}}=\frac{6+10 \sqrt{2}}{2}=3+5 \sqrt{2}$
$\sqrt{81 \times 2} \times \sqrt{16 \times 3}=9 \sqrt{2} \times 4 \sqrt{3}=36 \sqrt{6}$

## E: Indices

1) Write down the value of $9^{\frac{1}{2}} \sqrt{9}=3$
2) Work out the value of $\left(2^{2}\right)^{3} \quad 2^{6}=64$
3) Work out the value of $4^{-2}$

$$
\frac{1}{4^{2}}=\frac{1}{16}
$$

4) Write down the value of $49^{\frac{1}{2}} \sqrt{49}=7$
5) $7^{6} \times 7^{5}=7^{3} \times 7^{k}$, what is the value of $k$ ?
$76 \times 757^{11} \quad k=8$
6) Write down the reciprocal of 2

$$
\frac{1}{2}
$$

7) Work out $16^{\frac{3}{2}}$

$$
\left(16^{\frac{1}{2}}\right)^{3}=(\sqrt{16})^{3}=4^{3}=64
$$

8) Work out $64^{0}$

9) Work out $64^{-\frac{2}{3}}$
$\frac{1}{64^{23}}=\frac{1}{(643)^{2}}=\frac{1}{(\sqrt[364]{ })^{2}}=\frac{1}{4^{2}}=\frac{1}{16}$

F: Describing transformations
Describe fully the single transformation that maps one shape to the other - assume the shapes are mapped in alphabetical


1) Write 0.00037 in standard form

$$
3.7 \times 10^{-4}
$$

2) Write $8.25 \times 10^{3}$ as a normal number

## 8250

3) Work out $\left(2.1 \times 10^{8}\right) \times\left(6 \times 10^{-5}\right)$

$$
12.6 \times 10^{3}=1.26 \times 10^{4}
$$

4) Write $6.43 \times 10^{5}$ as an ordinary number

## 643000

5) Work out $2 \times 10^{7} \times 8 \times 10^{-12}$.

Give your answer in standard form.
$16 \times 10^{-5}=1.6 \times 10^{-4}$
6) Work out $\left(3 \times 10^{7}\right) \times\left(9 \times 10^{6}\right)$.

Give your answer in standard form.
$27 \times 10^{13}=2.7 \times 10^{14}$
7) What is the value of $\left(2.3 \times 10^{12}\right) \div\left(4.6 \times 10^{3}\right)$.

Give your answer in standard form.

$$
0.5 \times 10^{9}=5 \times 10^{8}
$$

8) Write $3 \times 10^{-5}$ as an ordinary number 0.00003

## H: Stratified sampling

1) Jenny is carrying out a survey for her GCSE Mathematics project.
She uses a stratified sample of 60 students according to year group.
Calculate the number of Year 11 students that should be in her sample

| Year group | 7 | 8 | 9 | 10 |
| :--- | :---: | :---: | :---: | :---: |
| Number of students | 190 | 145 | 145 | 1 |
| Total $=750$ |  |  |  |  |

$\frac{130}{750} \times 60=10 \cdot 4$10 shidents
2) An inspector wants to look at the work of a stratified sample of 70 of these students.
Find the number of students studying each of these languages that should be in the sample. Total $=650$

| Language | Number of students |  |
| :---: | :---: | :---: |
| Greek | 145 | cex ${ }^{2} 0=$ |
| Spanish | 121 |  |
| German | 198 |  |
| French | 186 | - 050 |


$150 \times 10=20.0 \rightarrow 20$ Gso
3) John wants to do a survey of the competitors.

He uses a stratified sample of exactly 50 competitors according to each age group.
Work out the number of competitors in each age group that should be in his stratified sample of 50 . Total $=570$


I: Percentage Change/Profit and Loss

1) Bytes is a shop that sells computers and digital cameras. In 2003, Bytes sold 620 computers. In 2004, Bytes sold 708 computers.

$$
708-620=88
$$

Work out the percentage increase in the number of computers sold. $\frac{88}{20} \times 100=14.2 \%$
2) In April 2004, the population of the European Community was 376 million.
In April 2005, the population of the European Community was 451 million.

$$
451-376=75
$$

Work out the percentage increase in population.
Give your answer correct to 1 decimal place.

$$
\times 100=19.9 \%
$$

3) Ishfaq bought a car for $£ 1500$ and later sold it for $£ 1350$. What percentage loss did Ishfaq make? $1500-1350=150$ $150.50 \times 100=10 \%$
4) Havar bought a car for $£ 8500$ and later sold it for $£ 7650$. What percentage loss did Havar make? $8500-7650=850$ $10 \%$
5) The table shows the number of mobile phones sold in a shop in April and in May.
Work out the percentage increase in the number of mobile phones sold from April to May.
Give your answer correct to 3 significant figures

| April | May |
| :---: | :---: |
| 85 | 91 |

$$
91-85=6
$$

$$
6 \times 100=7.06 \%
$$



J: Compound interest/Depreciation

1) Toby invested $£ 4500$ for 2 years in a savings account.

He was paid 4\% per annum compound interest.
How much did Toby have in his savings account after 2 years? $4500 \times 1.04^{2}=\$ 4867.20$
2) The value of a car depreciates by $35 \%$ each year. At the end of 2007 the value of the car was $£ 5460$ Work out the value of the car at the end of 2006 $5460 \times 0 \cdot 65=\neq 3549$

3) Mario invests $£ 2000$ for 3 years at $5 \%$ per annum compound interest.
Calculate the value of the investment at the end of 3 years. $2000 \times 1.05^{3}=ま 2315.25$
4) Derek invests $£ 154500$ for 2 years at $4 \%$ per year compound interest.
Work out the value of the investment at the end of 2 years. $154500 \times 1.04^{2}=\sum^{167107.20}$
5) A company bought a van that had a value of $£ 12000$

Each year the value of the van depreciates by $25 \%$.
Work out the value of the yon at the end of three years.
6) Liam invests $£ 6200$ for 3 years in a savings account.

He gets $2.5 \%$ per annum compound interest.
How much money will Liam have in his savings account at the end of 3 years? $6200 \times 1.025^{3}=\$ 6676.72$
7) Toby invested $£ 4500$ for 2 years in a savings account.

He was paid 4\% per annum compound interest.
How much did Toby have in his savings account after 2 years?

$$
4500 \times 1 \cdot 04^{2}=\neq 4867.20
$$

K: Reverse percentages

1) In a sale, normal prices are reduced by $20 \%$.

Andrew bought a saddle for his horse in the sale.
The sale price of the saddle was $£ 220$.
Calculate the normal price of the saddle.

$$
220 \div 0.8= \pm 275
$$

2) In a sale, normal prices are reduced by $15 \%$.

The sale price of a CD player is $£ 102$
Work out the normal price of the CD player.


$$
102 \% \cdot 0.85= \pm 120
$$

3) A garage sells cars.

It offers a discount of $20 \%$ off the normal price for cash.
Dave pays $£ 5200$ cash for a car.
Calculate the normal price of the car.

$$
5200 \div 0.8=+6500
$$

4) In a sale, normal prices are reduced by $25 \%$.

The sale price of a saw is $£ 12.75$
Calculate the normal price of the saw.

$$
12.75 \div 0.75=\neq 17
$$

5) In a sale, normal prices are reduced by $12 \%$.

The sale price of a DVD player is $£ 242$.
Work out the normal price of the DVD player.

$$
242 \div 0.88= \pm 275
$$

6) The price of all rail season tickets to London increased by $4 \%$. After the increase, the price of a rail season ticket from Brighton to London was $£ 2828.80$
Work out the price before this increase.

$$
2828.80 \div 1.04=\neq 2720
$$

## L: Mid-points and 3D Coordinates

Find the Midpoint of $A B$ for each pair of coordinates:

$$
A=(11,7) \text { and } B=(-7,9)(2,8)
$$

2) 

$$
A=(-9,6) \text { and } B=(1,-3)(-4,1 \cdot 5)
$$

If $M$ is the Midpoint of $A B$, find the coordinates of $A$ or $B$ :
3) $A=(-7,6)$ and $M=(3,3) B(13,0)$
4) $\quad M=(3,9)$ and $B=(5,7) A(1, \|)$

5) What are the coordinates of $A$ and $B$ ?
6) What are the coordinates of the mid-point, $M$, of $A B$ ?

$$
(2,5.5,1.5)
$$

M: Sectors

1) Calculate the area of the sector:
$\frac{150}{360} \times \pi \times 13^{2}=221.2 \mathrm{~cm}^{2}$

2) Work out the arc length $A B$ : $\frac{60}{360} x \pi \times 24=12 \cdot 6 \mathrm{~cm} \underbrace{12 \mathrm{~cm}}_{0}$
3) Work out the perimeter of the sector:
$\begin{aligned} & \text { Arc } \\ & \text { length }\end{aligned}=\frac{120}{360} \times \pi \times 12=12 \cdot 6 \mathrm{~cm}$

$60 \times \pi \times 12^{2}=75.4 \mathrm{~cm}^{2}$

N : Rearranging formulae

1) Make $p$ the subject of the formula $m=3 n+2 p$

$$
2 p=m-3 n \quad p=\frac{m-3 n}{2}
$$

2) Make $c$ the subject of the formula $a=3 c-4$

$$
3 c=a+4 \quad c=\frac{a+4}{3}
$$

3) Make $b$ the subject of the formula $\quad P=2 a+2 b$

$$
2 b=p-2 a \quad b=\frac{p-2 a}{2}
$$

4) Make $c$ the subject of the formula $f=3 c-4$

$$
3 C=f+4 \quad C=\frac{f+4}{3}
$$

5) Make $t$ the subject of the formula $u=7 t+30$

$$
7 t=u-30 \quad t=\frac{u-30}{7}
$$

6) Rearrange $y=\frac{1}{2} x+1$ to make $x$ the subject.

$$
\frac{1}{2} x=y-1 \quad x^{2}=2(y-1)
$$

7) Make $a$ the subject of the formula $s=\frac{a}{4}+8 u$

$$
\frac{a}{4}=s-8 u \quad a=4(s-8 u)
$$

8) Make $s$ the subject of the formula $v^{2}=u^{2}+2 a s$

$$
2 a s=v^{2}-u^{2} \quad S=\frac{v^{2}-u^{2}}{2 a}
$$

9) Make $u$ the subject of the formula $D=u t+k t^{2}$

$$
u t=D-k t^{2} \quad u=\frac{D-k t^{2}}{t}
$$

## O: Probability

1) The probability that a biased dice will land on a five is 0.3 Megan is going to roll the dice 400 times.
Work out an estimate for the number of times the dice will land on a five. $0.3 \times 400=120$
2) Jack sows 300 wildflower seeds.

The probability of a seed flowering is 0.7
Work out an estimate for the number of these seeds that will flower. $0.7 \times 300=210$
3) Four teams, City, Rovers, Town and United play a competition to win a cup. Only one team can win the cup. The table below shows the probabilities of City or Rovers or Town winning the cup.

| City | Rovers | Town | United |
| :--- | :--- | :--- | :--- |
| 0.38 | 0.27 | 0.15 | $x$ |

Work out the value of $x . \quad 1-(0.38+0.27+0.15)$
4) There are only red counters, blue counters, white counters and black counters in a bag. The table shows the probability that a counter taken at random from the bag will be red or blue.

| Colour | red | blue | white | black |
| :--- | :---: | :---: | :---: | :---: |
| Probability | 0.2 | 0.5 |  |  |

The number of white counters in the bag is the same as the number of black counters in the bag.

$$
1-(0.2+0.5)=0.3
$$ Work out the probability that Tania takes a white counter.

P: Prime factor form

1) Write 140 as the product of its prime factors. $2^{2} \times 5 \times 7$
2) Write 720 as a product of its prime factors. $2^{4} \times 3^{2} \times 5$
3) Find the Highest Common Factor of 60 and
96. $60=2^{2} \times 3 \times 5$ H.C.F $F=2^{2} \times 3=12$

$$
96=2^{5} \times 3
$$

4) Work out the Lowest Common Multiple of 60 and 96. L.G.M. $=25 \times 3 \times 5=480$
5) Find the Lowest Common Multiple of 120 and $150.120=28 \times 3 \times 5$

$$
\begin{aligned}
& 120=23 \times 3 \times 5 \\
& 150=2 \times 3 \times 5^{2}
\end{aligned}
$$

$$
L . C M=2 \times 3.30
$$

6) Express 108 as the product of powers of its prime factors. $2^{2} \times 3^{3}$
7) Work out the Highest Common Factor (HCF) of 24 and $64 \begin{aligned} & 24=23 \times 3 \\ & 64=26\end{aligned}$

$$
H \cdot C \cdot F=2^{3}=8
$$

8) Work out the Lowest Common Multiple (LCM) of 24 and 64

$$
L C \cdot M=2^{6} \times 3=192
$$

Q: Solving equations

1) Solve $2 t+8=3 \quad 2 t=-5 \quad t=-2 \cdot 5$
2) Solve $5 h+7=17 \quad 5 h=10 \quad h=2$
3) Solve $5 w-6=10 \quad 5 \mathrm{~W}=16 \quad \mathrm{~W}=\frac{16}{5}$
4) Solve

$$
\begin{aligned}
& 2 q+7=1 \\
& 2 q=-6 \quad q=-3 \\
& 5(t-3)=25 \\
& q=-3 \\
& 5 t-15=25 \quad 5 t=40 \quad t=8
\end{aligned}
$$

5) Solve
6) Solve

$$
\begin{aligned}
& 4(5 y-2)=48 \\
& 20 y=56 \quad y=\frac{56}{20}=\frac{14}{5} \\
& 13 x+1=11 x+9
\end{aligned}
$$

$$
20 y-8=48
$$

7) Solve

$$
\begin{aligned}
& 2 x=-8 \quad \frac{x=-4}{5 t-4=3 t+6} \\
& \text { olve }
\end{aligned}
$$

8) Solve
9) Solve

$$
\begin{aligned}
& 2 t=10 \quad \frac{t=5}{4 y}+3=2 y+8 \\
& \text { ve }
\end{aligned}
$$

10) Solve

$$
y=\frac{2 \cdot 5}{2 y+17=6 y+5}
$$

$$
4 y=12 \quad y=3
$$

R: Calculator use and Rounding
Work out the following.
Write down all the figures on your calculator display.

Round each answer to one significant figure.
Then round each answer to 2 decimal places.

## S: Inequalities

1) 

Solve the inequality $7 y-34 \leq 8$ $7 y \leqslant 42, y \leqslant 6$
Solve the inequality $4 x+1>11$ $4 x>10 \quad x>2.5$
3) Solve the inequality $4 t-5>11$ $4 t>16 \quad t>4$
4) Solve $3 y-2>13$
$3 y>15 \quad y>5$
Solve the inequality $3 p-7>11$ $3 p>18 \quad p>6$
6)

Solve $2 x-7 \leq 11$
$2 x \leqslant 18 \quad x \leqslant 9$
7) Solve the inequality $3(2 y+1)>10$ $6 y+3>10 \quad 6 y>7 \quad y>7 / 6$ Solve the inequality $4 x-3<7$ $4 x<10 \quad x<2.5$
9)

Write down the inequality shown:


T: Similar shapes

1) These shapes are mathematically similar.
a) Calculate the length of $B C 8 \times 1 \cdot 5=12 \mathrm{CM}$

2) These shapes are mathematically similar
a) Calculate the length of $Q R 12 \times 1 \cdot S=18 \mathrm{CM}$ b) Calculate the length of $A B$

3) These are similar solids.

Solid $A$ has a volume of $80 \mathrm{~cm}^{3}$, what is the volume of $B$ ? Solid $B$ has a surface area of $160 \mathrm{~cm}^{2}$, what is the surface area of $A$ ? L.S.F. $=2$
 A.S.F $=2^{2}=4$
V.S.F. $=2^{3}=8$

U: Upper and lower bounds

1) The weight of a bag of potatoes is 25 kg , correct to the nearest kg .
(a) Write down the smallest possible weight of the bag of potatoes. 24.5 kg
(b) Write down the largest possible weight of the bag of potatoes.

$$
25.5 \mathrm{~kg}
$$

2) A field is in the shape of a rectangle. The length of the field is 340 m , to the nearest metre. The width of the field is 117 m , to the nearest metre.
Calculate the upper bound for the perimeter of the field. $340.5+340.5+117.5+117.5$
$=916 \mathrm{~m}$
3) The length of a rectangle is 30 cm , correct to 2 significant figures.
The width of a rectangle is 18 cm , correct to 2 significant figures.
(a) Write down the upper bound of the width.
(b) Calculate the upper bound for the area of the rectangle $18.5 \times 30.5=564.25 \mathrm{~cm}^{2}$

## V: Substitution

## 1



## Take two $5 \mathrm{~m} l$ spoons full twice a day

You can work out the amount of medicine, $c \mathrm{ml}$, to give to a child by using the formula

$$
c=\frac{m a}{150}
$$

$m$ is the age of the child, in months. $a$ is an adult dose, in $\mathrm{m} l$.

A child is 30 months old.
An adult's dose is 40 ml .
Work out the amount of medicine you can give to the child.

$$
\begin{aligned}
& C=\frac{30 \times 40}{150}=\frac{1200}{150} \\
& =\frac{120}{120}=\frac{40}{8}=8 \mathrm{ml}
\end{aligned}
$$

$$
\begin{gathered}
\stackrel{2}{2} \\
A=\frac{h(x+10)}{2} \\
A=27 \quad 27=\frac{4(x+10)}{2} \\
h=4 \quad 54=4(x+10) \\
54=4 x+40 \quad x=\frac{14}{4}=3 \cdot 5 \\
4 x=14
\end{gathered}
$$

## W: Circle theorems



What is angle $A C D$ ? $54^{\circ}$
Give a reason for your answer. Angles @
2)

What is angle $A B C$ ? $84^{\circ}$ Give a reason for your o answer.
Angle @ centre is twice angle circumference
3)
 OBS? $90^{\circ}$ Tangent Monks padus ${ }_{G}$ your answer.
4)


What is angle BAD?
Give a reason for your answer.
opposite angles in acyclic quadrilateral sum to $180^{\circ}$
$X$ : Angles in Polygons
1)

2)


What is the exterior angle of a regular pentagon?

$$
\frac{360}{5}=72^{\circ}
$$

What is the interior angle of a regular hexagon? $360=60^{\circ} 180-60=120^{\circ}$ 6
3) The size of each exterior angle of a regular polygon is $40^{\circ}$.

Work out the number of sides of the regular polygon. 360 , $0=9$
4) The size of each interior angle of a regular polygon is $156^{\circ} .180-156=24 \quad 360 / 24=15$ Work out the number of sides of the polygon.
5) The diagram shows part of a regular 10-sided polygon.

Work out the size of the angle marked $x$.


$$
\begin{aligned}
& \frac{360}{10}=36 \quad 180-36 \\
&=144^{\circ}
\end{aligned}
$$

$y$ : Solve quadratics by factorising
Solve these quadratics by factorising:

$$
\begin{aligned}
x^{2}-4 x-45 & =0 \\
(x-9)(x+5) & =0 \quad x=9 \text { or } x=-5 \\
x^{2}-7 x+12 & =0 \\
(x-3)(x-4) & =0 \quad x=3 \text { or } x=4 \\
x^{2}-3 x-18 & =0 \\
(x-6)(x+3) & =0 \quad x=6 \text { or } x=-3 \\
x^{2}+6 x+8 & =0 \\
(x+4)(x+2)=0 \quad x & =-4 \text { or } x=-2 \\
x^{2}-x-56 & =0 \\
(x-8)(x+7)=0 \quad x & =8 \text { or } x=-7 \\
x^{2}+9 x+20 & =0 \\
(x+4)(x+5)=0 \quad x & =-4 \text { or } x=-5 \\
x^{2}+10 x+24 & =0 \\
(x+6)(x+4)=0 \quad x & =-6 \text { or } x=-4
\end{aligned}
$$

Z: Angles in Parallel Lines
Find the values of the missing angles.
Give reasons for your answers.
$180.47=7 x^{1}$ ate $\underset{\substack{\text { Diagram NoT } \\ \text { accurately draw }}}{ }$ angles an a shanght accurately drawn
min


