



MARKSCHEME

May 2014

MATHEMATICAL STUDIES

Standard Level

Paper 2

**Paper 2 Markscheme
Instructions to Examiners**

Notes: If in doubt about these instructions or any other marking issues, contact your team leader for clarification.

1 Abbreviations

M Marks awarded for **Method**

A Marks awarded for an **Answer** or for **Accuracy**

R Marks awarded for clear **Reasoning**

G Marks awarded for correct solutions obtained from a **Graphic Display Calculator**, when no working shown.

AG **Answer Given** in the question and consequently, marks not awarded.

ft Marks that can be awarded as **follow through** from previous results in the question.

2 Method of Marking

- (a) All marking must be done in scoris using the mathematical studies annotations and in accordance with the current document for guidance in e-marking Mathematical Studies SL. It is essential that you read this document before you start marking.
- (b) If a question part is completely correct use the number tick annotations to award full marks. If a part is completely wrong use the **A0** annotation, otherwise full annotations must be shown.
- (c) Working crossed out by the candidate should not be awarded any marks.
- (d) Where candidates have written two solutions to a question, only the first solution should be marked.
- (e) If correct working results in a correct answer but then further working is developed, full marks may **not** always be awarded. Full marks **will** be awarded if the candidate shows correct working leading to the correct answer. See also section 4(c).

Example: Calculate the gradient of the line passing through the points (5, 3) and (0, 9).

Markscheme	Candidates' Scripts	Marking
$\frac{9-3}{0-5} \quad (M1)$ <p>Award (M1) for correct substitution in gradient formula</p> $= -\frac{6}{5} \quad (A1)$	<p>(i) $\frac{9-3}{0-5} = -\frac{6}{5}$</p> <p>Gradient is $= -\frac{6}{5}$</p> <p style="text-align: right;"><i>(There is clear understanding of the gradient.)</i></p> $y = -\frac{6}{5}x + 9$	<p style="text-align: right;">(M1)</p> <p style="text-align: right;">(A1)</p>
	<p>(ii) $\frac{9-3}{0-5} = -\frac{6}{5}$</p> $y = -\frac{6}{5}x + 9$ <p style="text-align: right;"><i>(There is confusion about what is required.)</i></p>	<p style="text-align: right;">(M1)</p> <p style="text-align: right;">(A0)</p>

3 Follow-through (ft) Marks

Errors made at any step of a solution affect all working that follows. To limit the severity of the penalty, **follow through (ft)** marks can be awarded. Mark schemes will indicate where it is appropriate to apply follow through in a question with **‘(ft)’**.

- (a) Follow through applies only from one part of a question to a subsequent part of the question. Follow through does not apply within the same part.
- (b) If an answer resulting from follow through is extremely unrealistic (eg, negative distances or incorrect by large order of magnitude) then the final **A** mark should not be awarded.
- (c) If a question is transformed by an error into a **different, much simpler question** then follow through may not apply.
- (d) To award follow through marks for a question part, **there must be working present for that part**. An isolated follow through answer, without working is regarded as incorrect and receives no marks **even if it is approximately correct**.
- (e) The exception to the above would be in a question which is testing the candidate’s use of the GDC, where working will not be expected. **The markscheme will clearly indicate where this applies**.
- (f) Inadvertent use of radians will be penalised the first time it occurs. The markscheme will give clear instructions to ensure that only one mark per paper can be lost for the use of radians.

Example: Finding angles and lengths using trigonometry

Markscheme	Candidates’ Scripts	Marking
<p>(a) $\frac{\sin A}{3} = \frac{\sin 30}{4}$ (MI)(AI)</p> <p>Award (MI) for substitution in sine rule formula, (AI) for correct substitutions.</p> <p>$A = 22.0^\circ$ (22.0243...) (AI)(G2)</p>	<p>(a) $\frac{\sin A}{4} = \frac{\sin 30}{3}$</p> <p>$A = 41.8^\circ$</p> <p>(Note: the 2nd (AI) here was not marked (ft) and cannot be awarded because there was an earlier error in the same question part.)</p>	<p>(MI)(A0)</p> <p>(use of sine rule but with wrong values)</p> <p>(A0)</p>
<p>(b) $x = 7 \tan (22.0243\dots^\circ)$ (MI)</p> <p>$= 2.83$ (2.83163...) (AI)(ft)</p>	<p>(b) case (i) $x = 7 \tan 41.8^\circ$</p> <p>$= 6.26$</p> <p>but case (ii) 6.26</p>	<p>(MI)</p> <p>(AI)(ft)</p> <p>(G0)</p> <p>since no working shown</p>

4 Using the Markscheme

- (a) **A** marks are **dependent** on the preceding **M** mark being awarded, it is **not** possible to award **(M0)(A1)**. Once an **(M0)** has been awarded, all subsequent **A** marks are lost in that part of the question, even if calculations are performed correctly, until the next **M** mark.
The only exception to this will be for an answer where the accuracy is specified in the question – see section 5.
- (b) **A** marks are **dependent** on the **R** mark being awarded, it is **not** possible to award **(A1)(R0)**. Hence the **(A1)** cannot be awarded for an answer which is correct when no reason or the wrong reason is given.
- (c) In paper 2 candidates are expected to demonstrate their ability to communicate mathematics using appropriate working. Answers which are correct but not supported by adequate working will **not always receive full marks**, these unsupported answers are designated **G** in the mark scheme as an alternative to the full marks. Example **(M1)(A1)(A1)(G2)**.

Example: Using trigonometry to calculate an angle in a triangle.

Markscheme	Candidates' Scripts	Marking
<p>(a) $\frac{\sin A}{3} = \frac{\sin 30}{4}$ (M1)(A1) Award (M1) for substitution in sine rule formula, (A1) for correct substitutions. $A = 22.0^\circ$ (22.0243...) (A1)(G2)</p>	<p>(i) $\frac{\sin A}{3} = \frac{\sin 30}{4}$ $A = 22.0^\circ$</p> <p>(ii) $A = 22.0^\circ$ Note: G marks are used only if no working has been shown and the answer is correct.</p>	<p>(M1)(A1) (A1) (G2)</p>

- (d) **Alternative methods** may not always be included. Thus, if an answer is wrong then the working must be carefully analysed in order that marks are awarded for a different method consistent with the markscheme.
Where alternative methods for complete questions are included in the markscheme, they are indicated by '**OR**' etc.
- (e) Unless the question specifies otherwise, accept **equivalent forms**. For example: $\frac{\sin \theta}{\cos \theta}$ for $\tan \theta$.
On the markscheme, these equivalent numerical or algebraic forms will sometimes be written in brackets after the required answer.
Where numerical answers are required as the final answer to a part of a question in the markscheme, the scheme will show, in order:
the 3 significant figure answer worked through from full calculator display;
the exact value (for example $\sqrt{3}$ if applicable);
the full calculator display in the form 2.83163... as in the example above.
Where answers are given to 3 significant figures and are then used in subsequent parts of the question leading to a **different** 3 significant figure answer, these solutions will also be given.

- (f) As this is an international examination, all valid **alternative forms of notation** should be accepted. Some examples of these are:

Decimal points: 1.7; 1'7; 1·7; 1,7 .

Different descriptions of an interval: $3 < x < 5$; $(3, 5)$; $] 3, 5 [$.

Different forms of notation for set properties (eg, complement): A' ; \bar{A} ; A^c ; $U - A$; $(A; U \setminus A$.

Different forms of logic notation: $\neg p$; p' ; \tilde{p} ; \bar{p} ; $\sim p$.

$p \Rightarrow q$; $p \rightarrow q$; $q \Leftarrow p$.

- (g) Discretionary marks: There will be very rare occasions where the markscheme does not cover the work seen. In such cases the annotation DM should be used to indicate where an examiner has used discretion. Discretion should be used sparingly and if there is doubt and exception should be raised through scoris to the team leader.

As with previous sessions there will be no whole paper penalty marks for accuracy AP, financial accuracy FP and units UP. Instead these skills will be assessed in particular questions and the marks applied according to the rules given in sections 5, 6 and 7 below.

5 Accuracy of Answers

Incorrect accuracy should be penalized once only in each question according to the rules below.

Unless otherwise stated in the question, all numerical answers should be given exactly or correct to 3 significant figures.

1. If the candidate’s unrounded answer is seen and would round to the required 3 sf answer, then award *(AI)* and ignore subsequent rounding.
2. If the candidate’s unrounded answer is **not** seen then award *(AI)* if the answer given is **correctly** rounded to 2 or more significant figures, otherwise *(A0)*.
Note: If the candidate’s unrounded answer is **not** seen and the answer is given correct to 1 sf (correct or not), the answer will be considered wrong and will not count as incorrect accuracy. If this answer is used in subsequent parts, then working must be shown for further marks to be awarded.
3. If a correct 2 sf answer is used in subsequent parts, then working **must** be shown for further marks to be awarded. (This treatment is the same as for following through from an incorrect answer.)

These 3 points (see numbers in superscript) have been summarized in the table below and illustrated in the examples following.

	If candidates final answer is given ...				
	Exact or correct to 3 or more sf	Incorrect to 3 sf	Correct to 2 sf ³	Incorrect to 2 sf	Correct or incorrect to 1 sf
Unrounded answer seen ¹	Award the final <i>(AI)</i> irrespective of correct or incorrect rounding				
Unrounded answer not seen ²	<i>(AI)</i>	<i>(A0)</i>	<i>(AI)</i>	<i>(A0)</i>	<i>(A0)</i>
Treatment of subsequent parts	As per MS	Treat as follow through, only if working is seen ³			

Examples:

Markscheme	Candidates' Scripts	Marking
9.43 (9.43398...) (AI)	(i) 9.43398... is seen followed by 9; 9.4; 9.43; 9.434 <i>etc.</i> (correctly rounded)	(AI)
	(ii) 9.43398... is seen followed by 9.433; 9.44 <i>etc.</i> (incorrectly rounded)	(AI)
	(iii) 9.4	(AI)
	(iv) 9	(A0) (correct to 1 sf)
	(v) 9.3	(A0) (incorrectly rounded to 2 sf)
	(vi) 9.44	(A0) (incorrectly rounded to 3 sf)

Markscheme	Candidates' Scripts	Marking
7.44 (7.43798...) (AI)	(i) 7.43798... is seen followed by 7; 7.4; 7.44; 7.438 <i>etc.</i> (correctly rounded)	(AI)
	(ii) 7.43798... is seen followed by 7.437; 7.43 <i>etc.</i> (incorrectly rounded)	(AI)
	(iii) 7.4	(AI)
	(iv) 7	(A0) (correct to 1 sf)
	(v) 7.5	(A0) (incorrectly rounded to 2 sf)
	(vi) 7.43	(A0) (incorrectly rounded to 3 sf)

Example: ABC is a right angled triangle with angle $ABC = 90^\circ$, $AC = 32$ cm and $AB = 30$ cm. Find (a) the length of BC, (b) The area of triangle ABC.

Markscheme	Candidates' Scripts	Marking
(a) $BC = \sqrt{32^2 - 30^2}$ (MI) Award (MI) for correct substitution in Pythagoras' formula $= 11.1 (\sqrt{124}, 11.1355\dots)$ (AI)	(a) $BC = \sqrt{32^2 - 30^2}$ 11 (cm) (2 sf answer only seen, but correct)	(MI) (AI)
(b) $\text{Area} = \frac{1}{2} \times 30 \times 11.1355\dots$ (MI) Award (MI) for correct substitution in area of triangle formula $= 167(167.032\dots)$ (AI)(ft)	(b) case (i) $\text{Area} = \frac{1}{2} \times 30 \times 11$ $= 165 \text{ (cm}^2\text{)}$ case (ii) $= 165 \text{ (cm}^2\text{)}$	(MI) (working shown) (AI)(ft) (M0)(A0)(ft) (No working shown, the answer 11 is treated as a ft, so no marks awarded here)

Certain answers obtained from the GDC are worth 2 marks and working will not be seen. In these cases only one mark should be lost for accuracy.

eg, Chi-squared, correlation coefficient, mean

Markscheme	Candidates' Scripts	Marking
Chi-squared	(a) 7.7	(G2)
7.68 (7.67543...) (A2)	(b) 7.67	(G1)
	(c) 7.6	(G1)
	(d) 8	(G0)
	(e) 7	(G0)
	(e) 7.66	(G0)

Regression line

Markscheme	Candidates' Scripts	Marking
$y = 0.888x + 13.5$ (A2) ($y = 0.887686\dots x + 13.4895\dots$) If an answer is not in the form of an equation award at most (A1)(A0).	(a) $y = 0.89x + 13$	(G2) (both accepted)
	(b) $y = 0.88x + 13$	(G1) (one rounding error)
	(c) $y = 0.88x + 14$	(G1) (rounding error repeated)
	(d) (i) $y = 0.9x + 13$	(G1) (1 sf not accepted)
	(ii) $y = 0.8x + 13$	
(e) $0.88x + 13$	(G0) (one rounding error and not an equation)	

Maximum/minimum/points of intersection

Markscheme	Candidates' Scripts	Marking
(2.06, 4.49) (A1)(A1) (2.06020..., 4.49253...)	(a) (2.1, 4.5)	(A1)(A1) (both accepted)
	(b) (2.0, 4.4)	(A1) (same rounding error twice)
	(c) (2.06, 4.4)	(A1) (one rounding error)
	(d) (2, 4.4)	(A0) (1sf not accepted, one rounding error)

Rounding of an exact answer to 3 significant figures **should be accepted if performed correctly**.

Exact answers such as $\frac{1}{4}$ can be written as decimals to fewer than 3 significant figures if the result is still exact. Reduction of a fraction to its lowest terms is **not** essential, however where an answer simplifies to an integer this is expected.

Ratios of π and answers taking the form of square roots of integers or any rational power of an integer (eg, $\sqrt{13}, 2^{\frac{2}{3}}, \sqrt[4]{5}$), may be accepted as exact answers. All other powers (eg, of non-integers) and values of transcendental functions such as sine and cosine must be evaluated.

If the level of accuracy is specified in the question, a mark will be allocated for giving the answer to the required accuracy. In all such cases the final mark is not awarded if the rounding does not follow the instructions given in the question. A mark for specified accuracy can be regarded as a (ft) mark regardless of an immediately preceding (M0).

6 Level of accuracy in finance questions

The accuracy level required for answers will be specified in all questions involving money. This will usually be either whole units or two decimal places. The first answer not given to the specified level of accuracy will not be awarded the final **A** mark. The markscheme will give clear instructions to ensure that only one mark per paper can be lost for incorrect accuracy in a financial question.

Example: A financial question demands accuracy correct to 2 dp.

Markscheme	Candidates' Scripts	Marking
\$231.62 (231.6189) (AI)	(i) 231.6	(A0)
	(ii) 232	(A0) <i>(Correct rounding to incorrect level)</i>
	(iii) 231.61	(A0)
	(iv) 232.00	(A0) <i>(Parts (iii) and (iv) are both incorrect rounding to correct level)</i>

7 Units in answers

There will be specific questions for which the units are required and this will be indicated clearly in the markscheme. The first correct answer with no units or incorrect units will not be awarded the final **A** mark. The markscheme will give clear instructions to ensure that only one or two mark per paper can be lost for lack of units or incorrect units.

The units are considered only when the numerical answer is awarded **(AI)** under the accuracy rules given in Section 5.

Example:

Markscheme	Candidates' Scripts	Marking
(a) 37000 m ² (AI)	(a) 36000 m ²	(A0) <i>(Incorrect answer so units not considered)</i>
(b) 3200 m ³ (AI)	(b) 3200 m ²	(A0) <i>(Incorrect units)</i>

If no method is shown and the answer is correct but with incorrect or missing units award G marks with a one mark penalty.

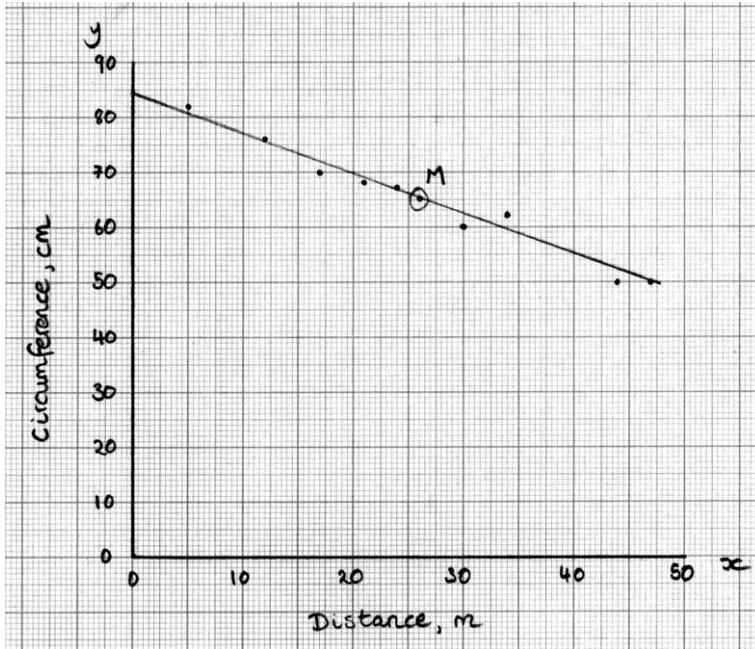
8 Graphic Display Calculators

Candidates will often be obtaining solutions directly from their calculators. They must use mathematical notation, not calculator notation. No method marks can be awarded for incorrect answers supported only by calculator notation. The comment 'I used my GDC' cannot receive a method mark.

1. (a) continuous

(A1) [1 mark]

(b)



(A1)(A1)(A1)(A1) [4 marks]

Notes: Award (A1) for labelled axes and correct scales; if axes are reversed award (A0) and follow through for their points. Award (A1) for at least 3 correct points, (A2) for at least 6 correct points, (A3) for all 9 correct points. If scales are too small or graph paper has not been used, accuracy cannot be determined; award (A0). Do not penalize if extra points are seen.

(c) (i) 26 (m)

(A1)

(ii) 65 (cm)

(A1) [2 marks]

(d) point M labelled, in correct position

(A1)(A1)(ft) [2 marks]

Notes: Award (A1)(ft) for point plotted in correct position, (A1) for point labelled M or (\bar{x}, \bar{y}) . Follow through from their answers to part (c).

(e) (i) -0.988 (-0.988432...)

(G2)

Note: Award (G2) for -0.99. Award (G1) for -0.990.
Award (A1)(A0) if minus sign is omitted.

(ii) $y = -0.756x + 84.7$ ($y = -0.756281\dots x + 84.6633\dots$)

(G2) [4 marks]

Notes: Award (A1) for $-0.756x$, (A1) for 84.7. If the answer is not given as an equation, award a maximum of (A1)(A0).

Question 1 continued

- (f) regression **line** through their M
regression **line** through their (0, 85) (accept 85 ± 1)

(A1)(ft)
(A1)(ft) [2 marks]

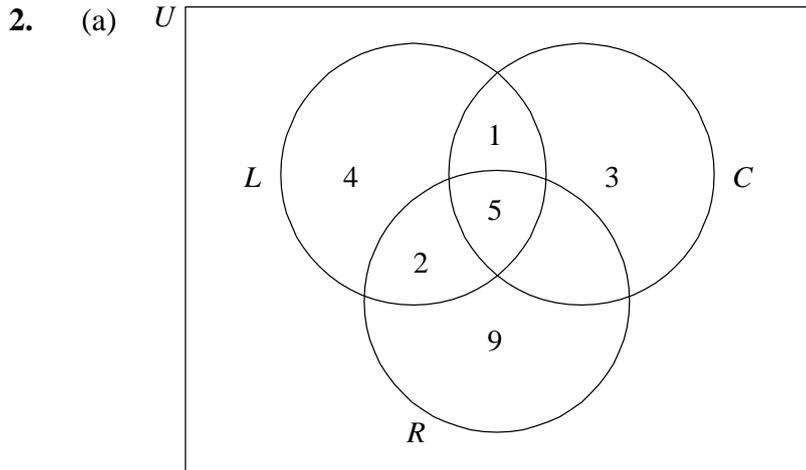
Notes: Follow through from part (d). Award a maximum of (A1)(A0) if the line is not straight. Do not penalize if either the line does not meet the y-axis or extends into quadrants other than the first. If M is not plotted or labelled, then follow through from part (c). Follow through from their y-intercept in part (e)(ii).

- (g) $-0.756281(40) + 84.6633$
 $= 54.4$ (cm) (54.4120...)

(M1)
(A1)(ft)(G2) [2 marks]

Notes: Accept 54.5 (54.46) for use of 3 sf. Accept 54.3 from use of -0.76 and 84.7 . Follow through from their equation in part (e)(ii) **irrespective of working shown**; the final answer seen must be consistent with that equation for the final (A1) to be awarded. Do not accept answers taken from the graph.

Total [17 marks]



(AI)(AI)(AI)(AI) [4 marks]

Note: Award (AI) for rectangle and three labelled intersecting circles (the rectangle need not be labelled), (AI) for 5, (AI) for 2 and 1, (AI) for 4, 3 and 9.

(b) $25 - (5 + 2 + 1 + 4 + 3 + 9)$ (MI)

Notes: Award (MI) for their $5 + 2 + 1 + 4 + 3 + 9$ seen even if total is greater than 25.
Do not award (AI)(ft) if their total is greater than 25.

$= 1$ (AI)(ft)(G2) [2 marks]

(c) (i) $\frac{12}{25}$ (0.48, 48%) (AI)(ft)(AI)(G2)

Notes: Award (AI)(ft) for numerator, (AI) for denominator.
Follow through from Venn diagram.

(ii) $\frac{16}{25}$ (0.64, 64%) (AI)(AI)(G2)

Notes: Award (AI) for numerator, (AI) for denominator.
There is no follow through; all information is given.

(iii) $\frac{4}{16}$ (0.25, 25%) (AI)(AI)(ft)(G2) [6 marks]

Notes: Award (AI) for numerator, (AI)(ft) for denominator.
Follow through from part (c)(ii) only.

(d) $\frac{6}{12}$ (0.5, 50%) (AI)(AI)(ft)(G2) [2 marks]

Notes: Award (AI) for numerator, (AI)(ft) for denominator.
Follow through from Venn diagram.

Total [14 marks]

3. (a) $600 + (20 - 1) \times 17$ (MI)(AI)

Note: Award (MI) for substituted arithmetic sequence formula, (AI) for correct substitutions. If a list is used, award (MI) for at least 6 correct terms seen, award (AI) for at least 20 correct terms seen.

$= 923$ (AI)(G3) [3 marks]

- (b) $\frac{10}{2} [2 \times 600 + (10 - 1) \times 17]$ (MI)(AI)

Note: Award (MI) for substituted arithmetic series formula, (AI) for their correct substitutions. Follow through from part (a). For consistent use of geometric series formula in part (b) with the geometric sequence formula in part (a) award a maximum of (MI)(AI)(A0) since their final answer cannot be an integer.

OR

$u_{10} = 600 + (10 - 1)17 = 753$ (MI)

$S_{10} = \frac{10}{2} (600 + \text{their } u_{10})$ (MI)

Note: Award (MI) for their correctly substituted arithmetic sequence formula, (MI) for their correctly substituted arithmetic series formula. Follow through from part (a) and **within** part (b).

Note: If a list is used, award (MI) for at least 10 correct terms seen, award (AI) for these terms being added.

$= 6765$ (accept 6770) (AI)(ft)(G2) [3 marks]

- (c) 3×2^9 (MI)(AI)

Note: Award (MI) for substituted geometric sequence formula, (AI) for correct substitutions. If a list is used, award (MI) for at least 6 correct terms seen, award (AI) for at least 8 correct terms seen.

$= 1536$ (AI)(G3) [3 marks]

Note: Exact answer only. If both exact and rounded answer seen, award the final (AI).

continued...

Question 3 continued

(d)
$$\frac{3 \times (2^8 - 1)}{2 - 1}$$

(MI)(AI)(ft)

Note: Award (MI) for substituted geometric series formula, (AI) for their correct substitutions. Follow through from part (c). If a list is used, award (MI) for at least 8 correct terms seen, award (AI) for these 8 correct terms being added. For consistent use of arithmetic series formula in part (d) with the arithmetic sequence formula in part (c) award a maximum of (MI)(AI)(AI).

$$= 765$$

(AI)(ft)(G2) [3 marks]

(e)
$$3 \times 2^{k-1} > 600 + (k - 1)(17)$$

(MI)

Note: Award (MI) for their correct inequality; allow equation. Follow through from parts (a) and (c). Accept sketches of the two functions as a valid method.

$$k > 8.93648\dots$$
 (may be implied)

(AI)(ft)

Note: Award (AI) for 8.93648... seen. The GDC gives answers of -34.3 and 8.936 to the inequality; award (MI)(AI) if these are seen with working shown.

OR

$$v_8 = 384 \quad u_8 = 719$$

(MI)

$$v_9 = 768 \quad u_9 = 736$$

(MI)

Note: Award (MI) for v_8 and u_8 both seen, (MI) for v_9 and u_9 both seen.

$$k = 9$$

(AI)(ft)(G2) [3 marks]

Note: Award (GI) for 8.93648... and -34.3 seen as final answer without working. Accept use of n .

Total [15 marks]

4. (a) $\frac{70}{\sin 78} = \frac{50}{\sin \hat{A}BC}$ (MI)(A1)

Note: Award (MI) for substituted sine rule, (A1) for correct substitution.

$\hat{A}BC = 44.3^\circ$ (44.3209...) (A1)(G3) [3 marks]

Note: If radians are used the answer is 0.375918..., award at most (MI)(A1)(A0).

(b) area $\Delta ABC = \frac{1}{2} \times 70 \times 50 \times \sin (57.6790\dots)$ (A1)(MI)(A1)(ft)

Notes: Award (A1)(ft) for their 57.6790... seen, (MI) for substituted area formula, (A1)(ft) for correct substitution.
Follow through from part (a).

$= 1480\text{m}^2$ (1478.86...) (A1)(ft)(G3) [4 marks]

Notes: The answer is 1480m^2 , units are required. 1479.20... if 3 sf used.
If radians are used the answer is $1554.11\dots\text{m}^2$, award (A1)(ft)(MI)(A1)(ft)(A1)(ft)(G3).

(c) $BM^2 = 70^2 + 25^2 - 2 \times 70 \times 25 \times \cos (57.6790\dots)$ (MI)(A1)(ft)

Notes: Award (MI) for substituted cosine rule, (A1)(ft) for correct substitution. Follow through from their angle in part (b).

$BM = 60.4(\text{m})$ (60.4457...) (A1)(ft)(G2) [3 marks]

Notes: If the 3 sf answer is used the answer is 60.5 (m).
If radians are used the answer is 62.5757...(m), award (MI)(A1)(ft)(A1)(ft)(G2).

continued...

Question 4 continued

(d) $\tan 63.4^\circ = \frac{TB}{60.4457...}$ (M1)

Note: Award (M1) for their correctly substituted trig equation.

$TB = 120.707...$ (A1)(ft)

Notes: Follow through from part (c). If 3 sf answers are used throughout, $TB = 120.815...$
If $TB = 120.707...$ is seen without working, award (A2).

$\tan \hat{NMB} = \frac{\left(\frac{120.707...}{2}\right)}{60.4457...}$ (A1)(ft)(M1)

Notes: Award (A1)(ft) for their TB divided by 2 seen, (M1) for their correctly substituted trig equation.
Follow through from part (c) and **within part (d)**.

$\hat{NMB} = 45.0^\circ$ (44.9563...) (A1)(ft)(G3)

Notes: If 3 sf are used throughout, answer is 45° .
If radians are used the answer is 0.308958..., and if full working is shown, award at most (M1)(A1)(ft)(A1)(ft)(M1)(A0).
If no working is shown for radians answer, award (G2).

OR

$\tan \hat{NMB} = \frac{NB}{BM}$ (M1)

$\tan 63.4^\circ = \frac{2 \times NB}{BM}$ (A1)(M1)

Note: Award (A1) for $2 \times NB$ seen.

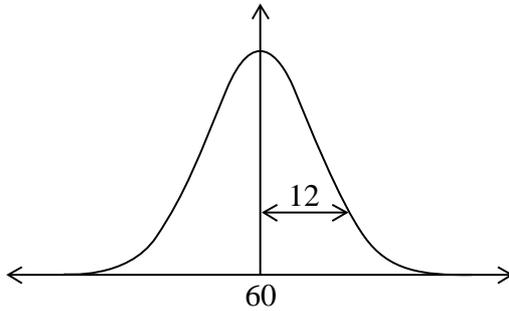
$\tan \hat{NMB} = \frac{1}{2} \tan 63.4^\circ$ (M1)

$\hat{NMB} = 45.0^\circ$ (44.9563...) (A1)(G3) [5 marks]

Notes: If radians are used the answer is 0.308958..., and if full working is shown, award at most (M1)(A1)(M1)(M1)(A0). If no working is shown for radians answer, award (G2).

Total [15 marks]

5. (a)



(A1)(A1) [2 marks]

Notes: Award (A1) for rough sketch of normal curve centred at 60, (A1) for some indication of 12 as the standard deviation *eg*, as diagram, or with 72 and 48 shown on the horizontal axis in appropriate places, or for 96 and 24 shown on the horizontal axis in appropriate places.

(b) $0.5 \left(\frac{1}{2}, 50\% \right)$

(A1) [1 mark]

Note: Accept only the exact answer.

(c) 0.0478 (0.0477903...)

(G2) [2 marks]

Note: Award (G1) for 0.952209..., award (M1)(G0) for diagram with correct area shown but incorrect answer.

(d) 0.955 (0.955434...)

(G2) [2 marks]

Note: Award (G1) for 0.044565..., award (M1)(G0) for diagram with correct area shown but incorrect answer.

(e) $0.0446 < 0.0478$

(R1)

Notes: Award (R1) for correct comparison seen. Accept alternative methods, for example, 1- (their answer to part (c)) used in comparison or a comparison based on *z* scores.

the Physics result is better

(A1)(ft) [2 marks]

Notes: Do not award (R0)(A1). Follow through from their answers to part (c) and part (d).

(f) 76

(G3) [3 marks]

Notes: Award (G1) for 75.8155..., award (G2) for 75.
Award (M1)(G0) for diagram with correct area shown but incorrect answer.

Total [12 marks]

6. (a) $2\pi r + 4r + 4l$ (AI)(AI)(AI) [3 marks]

Notes: Award (AI) for $2\pi r$ (“ π ” must be seen), (AI) for $4r$, (AI) for $4l$.
Accept equivalent forms. Accept $T = 2\pi r + 4r + 4l$. Award a maximum of (AI)(AI)(A0) if extra terms are seen.

- (b) $0.75 = \frac{\pi r^2 l}{2}$ (AI)(AI)(AI) [3 marks]

Notes: Award (AI) for their formula equated to 0.75, (AI) for l substituted into volume of cylinder formula, (AI) for volume of cylinder formula divided by 2.
If “ π ” not seen in part (a) accept use of 3.14 or greater accuracy.
Award a maximum of (AI)(AI)(A0) if extra terms are seen.

- (c) $T = 2\pi r + 4r + 4\left(\frac{1.5}{\pi r^2}\right)$ (AI)(ft)(AI)
 $= (2\pi + 4)r + \frac{6}{\pi r^2}$ (AG) [2 marks]

Notes: Award (AI)(ft) for correct rearrangement of their volume formula in part (b) seen, award (AI) for the correct substituted formula for T . The final line must be seen, with no incorrect working, for this second (AI) to be awarded.

- (d) $\frac{dT}{dr} = 2\pi + 4 - \frac{12}{\pi r^3}$ (AI)(AI)(AI) [3 marks]

Note: Award (AI) for $2\pi + 4$, (AI) for $\frac{-12}{\pi}$, (AI) for r^{-3} .
Accept 10.3 (10.2832...) for $2\pi + 4$, accept -3.82 $-3.81971...$ for $\frac{-12}{\pi}$. Award a maximum of (AI)(AI)(A0) if extra terms are seen.

continued...

Question 6 continued

(e) $2\pi + 4 - \frac{12}{\pi r^3} = 0$ OR $\frac{dT}{dr} = 0$ (M1)

Note: Award (M1) for setting their derivative equal to zero.

$r = 0.718843\dots$ OR $\sqrt[3]{0.371452\dots}$ OR $\sqrt[3]{\frac{12}{\pi(2\pi+4)}}$ OR $\sqrt[3]{\frac{3.81971}{10.2832\dots}}$ (A1)

$r = 0.719(\text{m})$ (AG) [2 marks]

Note: The rounded and unrounded or formulaic answers must be seen for the final (A1) to be awarded. The use of 3.14 gives an unrounded answer of $r = 0.719039\dots$

(f) $0.75 = \frac{\pi \times (0.719)^2 l}{2}$ (M1)

Note: Award (M1) for substituting 0.719 into their volume formula. Follow through from part (b).

$l = 0.924(\text{m})$ (0.923599...) (A1)(ft)(G2) [2 marks]

(g) $T = (2\pi + 4) \times 0.719 + \frac{6}{\pi(0.719)^2}$ (M1)

Notes: Award (M1) for substituting 0.719 in their expression for T . Accept alternative methods, for example substitution of their l and 0.719 into their part (a) (for which the answer is 11.08961024). Follow through from their answer to part (a).

$= 11.1(\text{m})$ (11.0880...) (A1)(ft)(G2) [2 marks]

Total [17 marks]