IB Questionbank Mathematical Studies 3rd edition

3D Trig MS

0 min 0 marks

1. (a)
$$l = \sqrt{8^2 + 8^2}$$
 (M1)
= $\sqrt{128}$
= 11.3 (3 s.f.) (A1)

(b)
$$L = \sqrt{\sqrt{128^2} + 8^2}$$
 OR $L = \sqrt{11.3^2 + 8^2}$ (allow ft from (a)) (M1)
= $\sqrt{128 + 64}$ **OR** = $\sqrt{127.69} + 64$
= 13.9 (3 s.f.) **OR** = 13.8 (3 s.f.) (A1)

2. (a)
$$\sqrt{5^2 + 1^2} = \sqrt{26}$$
 (or 5.10 (3 s.f.)) (M2)(A2) (C4)
(b) $\sqrt{4^2 + \sqrt{26}^2}$ (M2)
 $= \sqrt{42} = 6.48$ (3 s.f.) (A2) (C4)

[8]

[4]

3. (a)
$$AC = \sqrt{(22.5)^2 + 30^2}$$
 (M1)
= 37.5 cm (A1)

(b)
$$\tan G\hat{A}C = \frac{40}{37.5}$$
 (M1)

$$GAC = 46.8^{\circ}$$
 (or 0.818 radians)

Unit penalty applies in parts (a) and (b) 4.

(a)
$$AC^2 = 7.2^2 + 9.6^2$$
 (M1)
Note: Award (M1) for correct substitution in Pythagoras
Theorem.

$$AC = 12 m$$
 (A1) (C2)

(b)
$$AG^2 = 12^2 + 3.5^2$$
 (M1)
Note: Award (M1) for correct substitution in Pythagoras
Theorem.

(c)
$$\tan \theta = \frac{3.5}{12} \text{ or } \sin \theta = \frac{3.5}{12.5} \text{ or } \cos \theta = \frac{12}{12.5}$$
 (M1)

Note: Award (M1) for correct substitutions in trig ratio.

$$\theta = 16.3^{\circ}$$
 (A1)(ft) (C2)
Notes: Follow through from parts (a) and/or part (b) where

Notes: Follow through from parts (a) and/or part (b) where appropriate. Award (M1)(A0) for use of radians (0.284).

[6]

[4]

(A1)

5. Note: Unit penalty (UP) applies in part (a)

(a)
$$PB = \frac{1}{2}\sqrt{40^2 + 40^2} = \sqrt{800} = 28.28 (28.3)$$
 (M1)(A1)

Note: Award (M1) for correct substitutions, (A1) for correct answer.

UP
$$OB = \sqrt{40^2 + 28.28^2} = 49.0 \text{ cm} (\sqrt{2400} \text{ cm})$$
 (M1)(A1)(ft) (C4)
Note: Award (M1) for correct substitution, can (ft) from any
answer to PB.

UP

(b)
$$\sin^{-1}\left(\frac{40}{49}\right)$$

OR
 $\cos^{-1}\left(\frac{28.28}{49}\right)$
OR
 $\tan^{-1}\left(\frac{40}{28.28}\right)$ (M1)
= 54.7 (54.8) (A1)(ft) (C2)
Note: Award (M1) for any correct trig. ratio.
In radians = 0.616, award (M1)(A0).
Note: Common error: (a) OB = $\sqrt{40^2 + 20^2} = 44.7 \text{ cm}.$

Award (M0)(A0)(M1) (A1)(ft), and (b) angle OBP = 63.4° $(63.5^{\circ})(M1)(A1)(ft)$.

[6]

6. Unit penalty (UP) applies in parts (a) and (b) in this question.

(a)
$$VM^2 = 13^2 - 5^2$$
 (M1)
UP = 12 cm (A1) (C2)

(b)
$$h^2 = 12^2 - 5^2$$
 (or equivalent) (M1)
UP = 10.9 cm (A1)(ft) (C2)

(c)
$$\cos \theta = \frac{5}{12}$$
 (or equivalent) (M1)

$$\theta = 65.4^{\circ}$$
 (A1)(ft) (C2)

Note: Accept $\theta = 65.3^{\circ}$ (use of 10.9 with sine ratio).

[6]