# MARKSCHEME 

## May 2011

## MATHEMATICS

## Standard Level

## Paper 1

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## Instructions to Examiners

## Abbreviations

$\boldsymbol{M}$ Marks awarded for attempting to use a correct Method; working must be seen.
(M) Marks awarded for Method; may be implied by correct subsequent working.
$\boldsymbol{A} \quad$ Marks awarded for an Answer or for Accuracy; often dependent on preceding $\boldsymbol{M}$ marks.
(A) Marks awarded for an Answer or for Accuracy; may be implied by correct subsequent working.
$\boldsymbol{R} \quad$ Marks awarded for clear Reasoning.
$\boldsymbol{N} \quad$ Marks awarded for correct answers if no working shown.
$\boldsymbol{A} \boldsymbol{G}$ Answer given in the question and so no marks are awarded.

## Using the markscheme

## 1 General

Mark according to scoris instructions and the document "Mathematics SL: Guidance for e-marking
May 2011". It is essential that you read this document before you start marking. In particular, please note the following.

Marks must be recorded using the annotation stamps. Please check that you are entering marks for the right question.

- If a part is completely correct, (and gains all the 'must be seen' marks), use the ticks with numbers to stamp full marks.
- If a part is completely wrong, stamp $\boldsymbol{A 0}$ by the final answer.
- If a part gains anything else, it must be recorded using all the annotations.

All the marks will be added and recorded by scoris.

## 2 Method and Answer/Accuracy marks

- Do not automatically award full marks for a correct answer; all working must be checked, and marks awarded according to the markscheme.
- It is generally not possible to award $\boldsymbol{M 0}$ followed by $\boldsymbol{A 1}$, as $\boldsymbol{A}$ mark(s) depend on the preceding $\boldsymbol{M} \operatorname{mark}(\mathrm{s})$, if any. An exception to this rule is when work for $\boldsymbol{M} 1$ is missing, as opposed to incorrect (see point 4).
- Where $\boldsymbol{M}$ and $\boldsymbol{A}$ marks are noted on the same line, e.g. M1A1, this usually means $\boldsymbol{M 1}$ for an attempt to use an appropriate method (e.g. substitution into a formula) and $\boldsymbol{A 1}$ for using the correct values.
- Where there are two or more $\boldsymbol{A}$ marks on the same line, they may be awarded independently; so if the first value is incorrect, but the next two are correct, award A0A1A1.
- Where the markscheme specifies (M2), N3, etc., do not split the marks, unless there is a note. Once a correct answer to a question or part-question is seen, ignore further working.
- $\boldsymbol{M}$ marks are generally awarded for a valid attempt at answering the question. The working here does not need to be correct. In particular, where this is not the first $\boldsymbol{M}$ mark awarded, the markscheme may use the word "their", to indicate that even if there are previous errors, the $\boldsymbol{M}$ mark may still be awarded. A common example of this is where candidates need to derive an equation and then the markscheme says "attempt to solve their equation"; if their equation is wrong and as long as it is not simpler than the correct one, then the $\boldsymbol{M}$ mark is awarded.


## $N$ marks

If no working shown, award $\boldsymbol{N}$ marks for correct answers. In this case, ignore mark breakdown (M, $\boldsymbol{A}, \boldsymbol{R}$ ).

- Do not award a mixture of $\boldsymbol{N}$ and other marks.
- There may be fewer $\boldsymbol{N}$ marks available than the total of $\boldsymbol{M}, \boldsymbol{A}$ and $\boldsymbol{R}$ marks; this is deliberate as it penalizes candidates for not following the instruction to show their working.
- There may not be a direct relationship between the $N$ marks and the implied marks. There are times when all the marks are implied, but the $N$ marks are not the full marks: this indicates that we want to see some of the working, without specifying what.
- For consistency within the markscheme, $\boldsymbol{N}$ marks are noted for every part, even when these match the mark breakdown.
- If a candidate has incorrect working, which somehow results in a correct answer, do not award the $\boldsymbol{N}$ marks for this correct answer. However, if the candidate has indicated (usually by crossing out) that the working is to be ignored, award the $\boldsymbol{N}$ marks for the correct answer.


## Implied and must be seen marks

Implied marks appear in brackets e.g. (M1).

- Implied marks can only be awarded if correct/appropriate work is seen or implied in subsequent working. There are questions where some working is required, but as it is accepted that not everyone will write the same steps, all the marks are implied, but the $N$ marks are not the full marks for the question. (A correct final answer does not necessarily mean that the implied marks are all awarded).
- Normally the work is seen or implied in the next line.
- Where there is an (M1) followed by $\boldsymbol{A 1}$ for each correct value, if no working shown, one correct value is sufficient evidence to award the (M1).

Must be seen marks appear without brackets e.g. M1.

- Must be seen marks can only be awarded if correct/appropriate work is seen.
- If a must be seen mark is not awarded because work is missing (as opposed to $\boldsymbol{M 0}$ or $\boldsymbol{A 0}$ for incorrect work) all subsequent marks may be awarded if appropriate.


## Follow through marks (only applied after an error is made)

Follow through (FT) marks are awarded where an incorrect answer from one part of a question is used correctly in subsequent part(s) or subpart(s). Usually, to award FT marks, there must be working present and not just a final answer based on an incorrect answer to a previous part. However, if the only marks awarded in a subpart are for the answer (i.e. there is no working expected), then $\boldsymbol{F T}$ marks should be awarded if appropriate.

- Within a question part, once an error is made, no further $\boldsymbol{A}$ marks can be awarded for work which uses the error, but $\boldsymbol{M}$ marks may be awarded if appropriate. (However, as noted above, if an $\boldsymbol{A}$ mark is not awarded because work is missing, all subsequent marks may be awarded if appropriate).
- If the question becomes much simpler because of an error then use discretion to award fewer $\boldsymbol{F T}$ marks.
- If the error leads to an inappropriate value (e.g. probability greater than 1 , use of $r>1$ for the sum of an infinite GP, $\sin \theta=1.5$, non integer value where integer required), do not award the mark(s) for the final answer(s).
- Exceptions to this rule will be explicitly noted on the markscheme.
- If a candidate makes an error in one part, but gets the correct answer(s) to subsequent part(s), award marks as appropriate, unless the question says hence. It is often possible to use a different approach in subsequent parts that does not depend on the answer to previous parts.
- $\boldsymbol{F T}$ and "show that" questions : In a "show that" question, if an error leads to not showing the required answer, award $\boldsymbol{F T}$ marks as usual but do not award the final $\boldsymbol{A 1}$.

If a candidate incorrectly copies information from the question, this is a mis-read (MR). Apply a MR penalty of 1 mark to that question. Award the marks as usual and then stamp MR against the answer. Scoris will automatically deduct 1 mark from the question total. A candidate should be penalized only once for a particular mis-read. Do not stamp MR again for that question, unless the candidate makes another mis-read.

- If the question becomes much simpler because of the $\boldsymbol{M R}$, then use discretion to award fewer marks.
- If the $\boldsymbol{M R}$ leads to an inappropriate value (e.g. probability greater than 1 , use of $r>1$ for the sum of an infinite GP, $\sin \theta=1.5$, non integer value where integer required), do not award the mark(s) for the final answer(s).
- Miscopying of candidates' own work does not constitute a misread, it is an error.


## $7 \quad$ Discretionary marks (d)

An examiner uses discretion to award a mark on the rare occasions when the markscheme does not cover the work seen. The mark should be labelled (d) and a brief note written next to the mark explaining this decision.

## 8 <br> Alternative methods

Candidates will sometimes use methods other than those in the markscheme. Unless the question specifies a method, other correct methods should be marked in line with the markscheme. If in doubt, contact your team leader for advice.

- Alternative methods for complete questions are indicated by METHOD 1, METHOD 2, etc.
- Alternative solutions for part-questions are indicated by EITHER . . . OR.
- Where possible, alignment will also be used to assist examiners in identifying where these alternatives start and finish.


## 9 Alternative forms

Unless the question specifies otherwise, accept equivalent forms.

- As this is an international examination, accept all alternative forms of notation.
- In the markscheme, equivalent numerical and algebraic forms will generally be written in brackets immediately following the answer.
- In the markscheme, simplified answers, (which candidates often do not write in examinations), will generally appear in brackets. Marks should be awarded for either the form preceding the bracket or the form in brackets (if it is seen).


## 10 Accuracy of Answers

If the level of accuracy is specified in the question, a mark will be allocated for giving the answer to the required accuracy.

- Rounding errors: only applies to final answers not to intermediate steps.
- Level of accuracy: when this is not specified in the question the general rule applies to final answers: unless otherwise stated in the question all numerical answers must be given exactly or correct to three significant figures.

Candidates should be penalized once only IN THE PAPER for an accuracy error (AP). Award the marks as usual then stamp (AP) against the answer. Scoris will automatically deduct 1 mark from the paper total. Please see section E in the guidance document which clearly explains, with the use of screenshots, how this works in scoris.

- If a final correct answer is incorrectly rounded, apply the $\boldsymbol{A P}$.
- If the level of accuracy is not specified in the question, apply the $\boldsymbol{A P}$ for correct final answers not given to three significant figures.
- Intermediate values are sometimes written as $3.24(741$ ). This indicates that using 3.24 (or 3.25 ) is acceptable, but the more accurate value is 3.24741 . The digits in brackets are not required for the marks. If candidates work with fewer than three significant figures, this could lead to an $\boldsymbol{A P}$.
- Do not accept unfinished numerical answers such as $3 / 0.1$ (unless otherwise stated). As a rule, numerical answers with more than one part (such as fractions) should be given using integers (e.g. 6/8).

If there is no working shown, and there is an accuracy error (i.e. answers are given to the correct two significant figures, or incorrectly rounded but given to three significant figures), apply the $\boldsymbol{A P}$ with the $\boldsymbol{N}$ marks for these answers. However, do not accept answers to one significant figure without working.

## 11 Calculators

No calculator is allowed. The use of any calculator on paper 1 is malpractice, and will result in no grade awarded. If you see work that suggests a candidate has used any calculator, please follow the procedures for malpractice. Examples: finding an angle, given a trig ratio of 0.4235 .

## 12 Style

The markscheme aims to present answers using good communication, e.g. if the question asks to find the value of $k$, the markscheme will say $k=3$, but the marks will be for the correct value 3 - there is usually no need for the " $k=$ ". In these cases, it is also usually acceptable to have another variable, as long as there is no ambiguity in the question, e.g. if the question asks to find the value of $p$ and of $q$, then the student answer needs to be clear. Generally, the only situation where the full answer is required is in a question which asks for equations - in this case the markscheme will say "must be an equation".

The markscheme often uses words to describe what the marks are for, followed by examples, using the e.g. notation. These examples are not exhaustive, and examiners should check what candidates have written, to see if they satisfy the description. Where these marks are $\boldsymbol{M}$ marks, the examples may include ones using poor notation or incorrect work, to indicate what is acceptable.

## 13 Crossed out work

If a candidate has drawn a line through work on their examination script, or in some other way crossed out their work, do not award any marks for that work.

## 14 More than one solution

Where a candidate offers two or more different answers to the same question, the candidate knows one of the answers must be wrong or relatively inferior. This is likely to be an effort by the candidate to gain an advantage, hoping that the examiner will give credit for the right answer while the wrong or inferior answer is ignored. In such circumstances an examiner should only mark the first response unless the candidate indicates otherwise.

## SECTION A

1. (a) attempt to form composite
e.g. $g(7-2 x), 7-2 x+3$
$(g \circ f)(x)=10-2 x$
A1 [2 marks]
(b) $\quad g^{-1}(x)=x-3$

A1
N1 [1 mark]
(c) METHOD 1
valid approach
(M1)
e.g. $g^{-1}(5), 2, f(5)$
$f(2)=3$
A1
N2
[2 marks]
METHOD 2
attempt to form composite of $f$ and $g^{-1}$
(M1)
e.g. $\left(f \circ g^{-1}\right)(x)=7-2(x-3), 13-2 x$
$\left(f \circ g^{-1}\right)(5)=3$
A1
N2
[2 marks]

Total [5 marks]
2. (a) correct equation in the form $\boldsymbol{r}=\boldsymbol{a}+t \boldsymbol{b}$

$$
\boldsymbol{r}=\left(\begin{array}{c}
1 \\
-1 \\
2
\end{array}\right)+t\left(\begin{array}{c}
1 \\
3 \\
-2
\end{array}\right)
$$

(b) (i) attempt to substitute $t=2$ into the equation

$$
\begin{aligned}
& \text { e.g. }\left(\begin{array}{c}
2 \\
6 \\
-4
\end{array}\right),\left(\begin{array}{c}
1 \\
-1 \\
2
\end{array}\right)+2\left(\begin{array}{c}
1 \\
3 \\
-2
\end{array}\right) \\
& \overrightarrow{\mathrm{OP}}=\left(\begin{array}{c}
3 \\
5 \\
-2
\end{array}\right)
\end{aligned}
$$

(ii) correct substitution into formula for magnitude

$$
\begin{aligned}
& \text { e.g. } \sqrt{3^{2}+5^{2}+-2^{2}}, \sqrt{3^{2}+5^{2}+2^{2}} \\
& |\overrightarrow{\mathrm{OP}}|=\sqrt{38}
\end{aligned}
$$

A1
3. (a) $\operatorname{det} \boldsymbol{A}=2$
$\boldsymbol{A}^{-1}=\frac{1}{2}\left(\begin{array}{ll}3 & 4 \\ 1 & 2\end{array}\right)\left(=\left(\begin{array}{ll}\frac{3}{2} & 2 \\ \frac{1}{2} & 1\end{array}\right)\right)$
A1 N2
[2 marks]
(b) evidence of multiplying by $\boldsymbol{A}^{-1}$
e.g. $\quad \boldsymbol{X}=\boldsymbol{A}^{-1}\left(\begin{array}{cc}4 & 6 \\ 2 & -2\end{array}\right), \boldsymbol{A}^{-1} \boldsymbol{B}$
correct working
e.g. $\boldsymbol{X}=\frac{1}{2}\left(\begin{array}{ll}3 & 4 \\ 1 & 2\end{array}\right)\left(\begin{array}{cc}4 & 6 \\ 2 & -2\end{array}\right),\left(\begin{array}{cc}\frac{3}{2} & 2 \\ \frac{1}{2} & 1\end{array}\right)\left(\begin{array}{cc}4 & 6 \\ 2 & -2\end{array}\right), \frac{1}{2}\left(\begin{array}{cc}20 & 10 \\ 8 & 2\end{array}\right)$

$$
\boldsymbol{X}=\left(\begin{array}{rr}
10 & 5 \\
4 & 1
\end{array}\right)
$$

4. (a) $\mathrm{P}(X=2)=\frac{4}{14} \quad\left(=\frac{2}{7}\right)$
(b) $\quad \mathrm{P}(X=1)=\frac{1}{14}$
$\mathrm{P}(X=k)=\frac{k^{2}}{14}$
setting the sum of probabilities $=1$ M1
e.g. $\frac{1}{14}+\frac{4}{14}+\frac{k^{2}}{14}=1,5+k^{2}=14$
$k^{2}=9 \quad\left(\operatorname{accept} \frac{k^{2}}{14}=\frac{9}{14}\right)$
$k=3$
AG
(c) correct substitution into $\mathrm{E}(X)=\sum x \mathrm{P}(X=x)$
e.g. $1\left(\frac{1}{14}\right)+2\left(\frac{4}{14}\right)+3\left(\frac{9}{14}\right)$
$\mathrm{E}(X)=\frac{36}{14} \quad\left(=\frac{18}{7}\right)$
5. (a) $\frac{\mathrm{d}}{\mathrm{d} x} \ln x=\frac{1}{x}, \frac{\mathrm{~d}}{\mathrm{~d} x} x^{2}=2 x$ (seen anywhere) A1A1
attempt to substitute into the quotient rule (do not accept product rule)
e.g. $\frac{x^{2}\left(\frac{1}{x}\right)-2 x \ln x}{x^{4}}$
correct manipulation that clearly leads to result A1
e.g. $\frac{x-2 x \ln x}{x^{4}}, \frac{x(1-2 \ln x)}{x^{4}}, \frac{x}{x^{4}}-\frac{2 x \ln x}{x^{4}}$
$g^{\prime}(x)=\frac{1-2 \ln x}{x^{3}}$
$A \boldsymbol{G}$
N0
[4 marks]
(b) evidence of setting the derivative equal to zero (M1)
e.g. $g^{\prime}(x)=0,1-2 \ln x=0$
$\ln x=\frac{1}{2}$
$x=\mathrm{e}^{\frac{1}{2}}$

A1
[3 marks]

## 6. METHOD 1

using double-angle identity (seen anywhere)
e.g. $\sin 2 x=2 \sin x \cos x, 2 \cos x=2 \sin x \cos x$
evidence of valid attempt to solve equation
e.g. $\quad 0=2 \sin x \cos x-2 \cos x, 2 \cos x(1-\sin x)=0$
$\cos x=0, \sin x=1$ A1A1
$x=\frac{\pi}{2}, x=\frac{3 \pi}{2}, x=\frac{5 \pi}{2}$

## METHOD 2



A1A1M1A1
Notes: Award $\boldsymbol{A 1}$ for sketch of $\sin 2 x, \boldsymbol{A 1}$ for a sketch of $2 \cos x, \boldsymbol{M 1}$ for at least one intersection point seen, and $\boldsymbol{A 1}$ for 3 approximately correct intersection points. Accept sketches drawn outside [ $0,3 \pi$ ], even those with more than 3 intersections.

$$
x=\frac{\pi}{2}, x=\frac{3 \pi}{2}, x=\frac{5 \pi}{2}
$$

7. (a) valid approach
(M1)
e.g. $b^{2}-4 a c, \Delta=0,(-4 k)^{2}-4(2 k)(1)$
correct equation
A1
e.g. $(-4 k)^{2}-4(2 k)(1)=0,16 k^{2}=8 k, 2 k^{2}-k=0$
correct manipulation
A1
e.g. $8 k(2 k-1), \frac{8 \pm \sqrt{64}}{32}$
$k=\frac{1}{2}$
N3
$\begin{array}{ll}\text { (b) recognizing vertex is on the } x \text {-axis } \\ \text { e.g. }(1,0) \text {, sketch of parabola opening upward from the } x \text {-axis } & \text { M1 } \\ p \geq 0 & \boldsymbol{A 1}\end{array}$
[5 marks]

## SECTION B

8. (a) (i) $s=1$
(ii) evidence of appropriate approach

A1
N1
(M1)
e.g. $21-16,12+8-q=15$
$q=5$
A1 N2
(iii) $p=7, r=3$

A1A1
$N 2$
[5 marks]
(b) (i) $\quad \mathrm{P}($ art $\mid$ music $)=\frac{5}{8}$
(ii) METHOD 1
$\mathrm{P}($ art $)=\frac{12}{16} \quad\left(=\frac{3}{4}\right)$
A1
evidence of correct reasoning R1
e.g. $\frac{3}{4} \neq \frac{5}{8}$
the events are not independent
$A G$
METHOD 2
$\mathrm{P}($ art $) \times \mathrm{P}($ music $)=\frac{96}{256}\left(=\frac{3}{8}\right)$
A1
evidence of correct reasoning
R1
e.g. $\frac{12}{16} \times \frac{8}{16} \neq \frac{5}{16}$
the events are not independent
$A G$
No
[4 marks]
(c) $\quad \mathrm{P}$ (first takes only music) $=\frac{3}{16}$ (seen anywhere)

A1

A1
evidence of valid approach
e.g. $\frac{3}{16} \times \frac{7}{15}$
$\mathrm{P}($ music and art $)=\frac{21}{240} \quad\left(=\frac{7}{80}\right)$
9. (a) (i) $\overrightarrow{\mathrm{BA}}=\left(\begin{array}{l}3 \\ 0 \\ 4\end{array}\right)$

A1
N1
(ii) evidence of combining vectors
e.g. $\overrightarrow{\mathrm{AB}}+\overrightarrow{\mathrm{BC}}=\overrightarrow{\mathrm{AC}}, \overrightarrow{\mathrm{BA}}+\overrightarrow{\mathrm{AC}},\left(\begin{array}{c}-2 \\ 2 \\ -6\end{array}\right)-\left(\begin{array}{c}-3 \\ 0 \\ -4\end{array}\right)$
$\overrightarrow{\mathrm{BC}}=\left(\begin{array}{c}1 \\ 2 \\ -2\end{array}\right)$

## (b) (i) METHOD 1

finding $\overrightarrow{\mathrm{BA}} \cdot \overrightarrow{\mathrm{BC}},|\overrightarrow{\mathrm{BA}}|,|\overrightarrow{\mathrm{BC}}|$
(A1)(A1)(A1)
e.g. $\overrightarrow{\mathrm{BA}} \cdot \overrightarrow{\mathrm{BC}}=3 \times 1+0+4 \times-2,|\overrightarrow{\mathrm{BA}}|=\sqrt{3^{2}+4^{2}},|\overrightarrow{\mathrm{BC}}|=3$
substituting into formula for $\cos \theta$
M1
e.g. $\frac{3 \times 1+0+4 \times-2}{3 \sqrt{3^{2}+0+4^{2}}}, \frac{-5}{5 \times 3}$
$\cos \mathrm{A} \hat{\mathrm{B}} \mathrm{C}=-\frac{5}{15}\left(=-\frac{1}{3}\right)$

## METHOD 2

finding $|\overrightarrow{A C}|,|\overrightarrow{B A}|,|\overrightarrow{B C}|$
(A1)(A1)(A1)
e.g. $|\overrightarrow{\mathrm{AC}}|=\sqrt{2^{2}+2^{2}+6^{2}},|\overrightarrow{\mathrm{BA}}|=\sqrt{3^{2}+4^{2}},|\overrightarrow{\mathrm{BC}}|=3$
substituting into cosine rule
M1
e.g. $\frac{5^{2}+3^{2}-(\sqrt{44})^{2}}{2 \times 5 \times 3}, \frac{25+9-44}{30}$
$\cos \mathrm{A} \hat{\mathrm{B}} \mathrm{C}=-\frac{10}{30}\left(=-\frac{1}{3}\right)$
A1
(ii) evidence of using Pythagoras
$e . g$. right-angled triangle with values, $\sin ^{2} x+\cos ^{2} x=1$
$\sin A \hat{B} C=\frac{\sqrt{8}}{3} \quad\left(=\frac{2 \sqrt{2}}{3}\right)$

## Question 9 continued

(c) (i) attempt to find an expression for $|\overrightarrow{C D}|$
e.g. $\sqrt{(-4)^{2}+5^{2}+p^{2}},|\overrightarrow{\mathrm{CD}}|^{2}=4^{2}+5^{2}+p^{2}$
correct equation
e.g. $\sqrt{(-4)^{2}+5^{2}+p^{2}}=\sqrt{50}, 4^{2}+5^{2}+p^{2}=50$
$p^{2}=9$
A1
$p=3 \quad \boldsymbol{A G}$
N0
(ii) evidence of scalar product (M1)
e.g. $\left(\begin{array}{c}-4 \\ 5 \\ 3\end{array}\right) \cdot\left(\begin{array}{c}1 \\ 2 \\ -2\end{array}\right), \overrightarrow{\mathrm{CD}} \cdot \overrightarrow{\mathrm{BC}}$
correct substitution
e.g. $-4 \times 1+5 \times 2+3 \times-2,-4+10-6 \quad$ A1
$\overrightarrow{\mathrm{CD}} \cdot \overrightarrow{\mathrm{BC}}=0 \quad$ A1
$\overrightarrow{\mathrm{CD}}$ is perpendicular to $\overrightarrow{\mathrm{BC}} \quad \boldsymbol{A G}$
10. (a) $v=1$ A1 N1
(b) (i) $\quad \frac{\mathrm{d}}{\mathrm{d} t}(2 t)=2$
$\frac{\mathrm{d}}{\mathrm{d} t}(\cos 2 t)=-2 \sin 2 t$
Note: Award $\boldsymbol{A 1}$ for coefficient 2 and $\boldsymbol{A 1}$ for $-\sin 2 t$
evidence of considering acceleration $=0$
(MI)
e.g. $\frac{\mathrm{d} v}{\mathrm{~d} t}=0,2-2 \sin 2 t=0$
correct manipulation
e.g. $\sin 2 k=1, \sin 2 t=1$

$$
2 k=\frac{\pi}{2} \quad\left(\operatorname{accept} 2 t=\frac{\pi}{2}\right)
$$

$$
k=\frac{\pi}{4}
$$

(ii) attempt to substitute $t=\frac{\pi}{4}$ into $v$
e.g. $2\left(\frac{\pi}{4}\right)+\cos \left(\frac{2 \pi}{4}\right)$ $v=\frac{\pi}{2}$ A1

## Question 10 continued

(c)


A1A1A2
Notes: Award $\boldsymbol{A 1}$ for $y$-intercept at $(0,1), \boldsymbol{A 1}$ for curve having zero gradient at $t=\frac{\pi}{4}$, $\boldsymbol{A} 2$ for shape that is concave down to the left of $\frac{\pi}{4}$ and concave up to the right of $\frac{\pi}{4}$. If a correct curve is drawn without indicating $t=\frac{\pi}{4}$, do not award the second $\boldsymbol{A 1}$ for the zero gradient, but award the final $\boldsymbol{A} 2$ if appropriate.

Sketch need not be drawn to scale. Only essential features need to be clear.
(d) (i) correct expression

A2
e.g. $\int_{0}^{1}(2 t+\cos 2 t) \mathrm{d} t,\left[t^{2}+\frac{\sin 2 t}{2}\right]_{0}^{1}, 1+\frac{\sin 2}{2}, \int_{0}^{1} v \mathrm{~d} t$
(ii)


Note: The line at $t=1$ needs to be clearly after $t=\frac{\pi}{4}$.

