MARK SCHEME for the October/November 2013 series

0606 ADDITIONAL MATHEMATICS

0606/11

Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the October/November 2013 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.



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Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Accuracy mark for a correct result or statement independent of method marks.
- When a part of a question has two or more 'method' steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √^h implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously 'correct' answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
 B2, 1, 0 means that the candidate can earn anything from 0 to 2.

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1	a = 3, b = 2,	<i>c</i> = 1	B1, B1 B1	, [3]	B1 for	each	
2	Using $b^2 - 4ac$ $4k^2 + 8k -$	$9 = 4 (k + 1)^{2}$ - 5 = 0	M1 DM1			any use of $b^2 - 4ac$ or solution of their	quadratic in k
	$k=-\frac{5}{2},$	$\left(\frac{1}{2}\right)$	A1		A1 for	critical value(s), $\frac{1}{2}$	not necessary
	To be below the	the x-axis $k < -\frac{5}{2}$	A1	[4]	A1 for	$k < -\frac{5}{2}$ only	
	To lie under th $\therefore (k+1)\frac{9}{4(k+1)}$	$x = \frac{3}{2(k+1)}$ $\frac{9}{(k+1)^2} - \frac{9}{2(k+1)} + (k+1)$ e x-axis, y < 0 $\frac{1}{1} - \frac{9}{2(k+1)} + (k+1) < 0$ $4(k+1)^2 \text{ or equivalent}$	M1		M1 for	a complete method	l to this point.

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Γ				1			
	3 $\frac{1+\sin\theta}{\cos\theta} + \frac{\cos\theta}{1+\sin\theta} + \frac{(1+\sin\theta)^2 + \cos^2\theta}{\cos\theta(1+\sin\theta)}$ $= \frac{1+2\sin\theta + \sin^2\theta + \cos^2\theta}{\cos\theta(1+\sin\theta)}$			M1 for dealing with the fractions, denominator must be correct, be gener- with numerator			
$=\frac{2+2}{\cos\theta(1)}$	DM1			M1 for expansion and use of $\cos^2 \theta + \sin^2 \theta = 1$			
$=\frac{2(1+)}{\cos\theta(1+)}$	$\frac{\sin \theta}{+\sin \theta}$	DM1		M1 for	attempt to factoris	se	
$=2 \sec \theta$				A1 for	obtaining final ans	swer correctly	
$= \frac{(\sec \theta + t)}{\sec \theta}$ $= \frac{\sec^2 \theta + t}{\cos^2 \theta}$	$\theta + \frac{1}{\sec \theta + \tan \theta}$	M1 DM1			dealing with the f		
$=\frac{2\sec\theta(\sec\theta)}{\sec\theta}$	$\frac{\theta + \tan \theta}{\det \theta + \tan \theta}$	DM1		$\tan^2 \theta$ DM1 f	M1 for expansion and use of $\tan^2 \theta + 1 = \sec^2 \theta$ DM1 for attempt to factorise		
$=2 \sec \theta$		A1		A1 for	obtaining final ans	btaining final answer correctly	
4 (i) n (<i>A</i>) = 3		B1	[1]	correct $n(A) =$	ents listed for (i), t elements to get B 3. If they are not l given then B1.	1 leading to	
(ii) n (<i>B</i>) = 4		B1	[1]	correct B1. If	ents listed for (ii), elements leading t they are not listed a hen B1.		
(iii) $A \cup B = \{$	{60°, 240°, 300, 420°, 600°}	√B1	[1]	Follow through on any sets listed in (i) an (ii). Do not allow any repetitions.			
(iv) $A \cap B = \{$	{60°, 420°}	√B1	[1]	Follow (ii).	through on any se	ts listed in (i) and	

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5 (i) $9x - \frac{1}{3}co$	s3x(+c)	B1, B1, B1 [3]	B1 for 9x, B1 for $\frac{1}{3}$ or cos3x B1 for $-\frac{1}{3}$ cos3x Condone omission of + c			
(ii) $\left[9x - \frac{1}{3}c\right]$	$\cos 3x \bigg]_{\frac{\pi}{9}}^{\pi}$					
$=\left(9\pi-\frac{1}{3}\right)$	$\frac{1}{3}\cos 3\pi \left(-\frac{1}{3}\cos \frac{\pi}{3} \right)$	M1	M1 for to (i)	correct use of limi	ts in their answer	
$=8\pi+\frac{1}{2}$		A1, A1 [3]	A1 for	each term		
$6 \qquad \mathbf{f}\left(\frac{1}{2}\right) = \frac{a}{8} + 1$	$+\frac{b}{2}-2$	M1	M1 for	substitution of x =	$=\frac{1}{2}$ into f (x)	
leading to $a +$	4b - 8 = 0	A1	A1 for	correct equation in	any form	
f(2) = 2f(-1)		M1		attempt to substitution into $f(x)$ and use $f(x) + f(x)$		
8a + 16 + 2b -	-2 = 2(-a + 4 - b - 2)	A1		a correct equation $\pm 1(-1)$	in any form	
leading to $10a$ $\therefore a = -2, b$	+4b+10 = 0 or equivalent = $\frac{5}{2}$	DM1 A1 [6]	attemp obtain	on both previous N t to solve simultance either <i>a</i> or <i>b</i> both correct		

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7 (a)	(ii) 120)	B1 [1] 1]					
(b)	(i) 924(ii) 28	ł	B1	1] 1]					
		$4 - ({}^{8}C_{3} \times {}^{4}C_{3}) - ({}^{8}C_{2} \times {}^{4}C_{4})$ 4 - 3M 3W - 2M 4W)	M1		t 3 terms, at least 2 t in terms of C nota				
924 - 224 - 28 = 672					any pair (must be final answer	evaluated)			
Or:		${}^{8}C_{4} \times {}^{4}C_{2} = 420$	M1		M1 for 3 terms, at least 2 of which must b correct in terms of <i>C</i> notation or evaluated				
		${}^{8}C_{5} \times {}^{4}C_{1} = 224$ ${}^{8}C_{6} = 28$	A1		A1 for any pair (must be evaluated)				
		Total = 672	A1	A1 for	A1 for final answer				
8 (i)			B1 B1		correct shape (-3, 0) or -3 seen	on graph			
			B1		(2, 0) or 2 seen on				
			B1	4]	(0, 6) or 6 seen on	graph or in a table			
(ii)	$\left(-\frac{1}{2},\frac{25}{4}\right)$.)	B1, B1	B1 for	each				
(iii)	$k > \frac{25}{4}$ or	$r \frac{25}{4} < k \ (\leq 14)$	B1 [1]					

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9	(a) $12x^2\ln(2$	$(x+1) + 4x^3 \left(\frac{2}{2x+1}\right)$	M1 A2, 1, 0 [3]	M1 for -1 for e	correct product	
	(b) (i) $\frac{dy}{dy}$	$\frac{1}{x} = \frac{(x+2)^{\frac{1}{2}} 2 - 2x(x+2)^{-\frac{1}{2}} \frac{1}{2}}{x+2}$	M1, A1		differentiation of a ng $(x+2)^{\frac{1}{2}}$	quotient
		$=\frac{(x+2)^{-\frac{1}{2}}}{(x+2)}(2(x+2)-x)$	DM1		correct unsimplified or attempt to simpli	
	=	$\frac{x+4}{\left(x+2\right)^{\frac{3}{2}}}$	A1 [4]	A1 for given a	correct simplifications in the second s	on to obtain the
	$\mathbf{Or:} \\ \frac{\mathrm{d}y}{\mathrm{d}x} = 2x \bigg($	$\left[-\frac{1}{2}\right](x+2)^{-\frac{3}{2}} + (x+2)^{-\frac{1}{2}}(2)$	M1, A1		differentiation of a ng $(x+2)^{-\frac{1}{2}}$	product
	$=$ $\frac{x}{x}$	$(+2)^{-\frac{3}{2}}(2(x+2)-x) + \frac{4}{(x+2)^{\frac{3}{2}}}$	DM1 A1	DM1 fo	correct unsimplified or attempt to simpli correct simplification nswer	fy
	(ii) $\frac{10x}{\sqrt{x+2}}$ ((+c)	M1,A1 [2]	A1 com	$\frac{1}{5} \times \frac{2x}{\sqrt{x+2}} \text{ or } 5 \times \frac{2x}{\sqrt{x+2}}$ or $5 \times \frac{2x}{\sqrt{x+2}}$ or $\frac{2x}{\sqrt{x+2}}$	
	(iii) $\left[\frac{10x}{\sqrt{x+2}}\right]$		M1		correct application to (b)(ii)	of limits in their
		$=\frac{40}{3}$	A1 [2]			

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10 (i) $\sqrt{20}$ or 4.	47	B1 [1]				
(ii) Grad <i>AB</i> =	M1	M1 for	attempt at a perp g	gradient		
⊥line y	y - 4 = -2(x - 1)	M1, A1	M1 for attempt at straight line equation, must be perpendicular and passing through <i>B</i> .			
(y = -2x +	- 6)	[3]	-	ow unsimplified		
$(x-1)^2 +$	f C (x, y) and BC ² = 20 (y - 4) ² = 20 or f C (x y) and AC ² = 40	M1	M1 for attempt to obtain relationship using an appropriate length and the point $(1, 4)$ or (-3, 2)			
$(x+3)^2 +$	f C (x, y) and AC ² = 40 (y-2) ² = 40	A1	A1 for a correct equation			
Need inte	rsection with $y = -2x + 6$,	DM1	DM1 for attempt to solve with $y = -2x + 6$ and obtain a quadratic equation in terms of one variable only			
leads to 5. $5y^2 - 40y$	$x^2 - 10x - 15 = 0 $ or -= 0			-		
giving $x =$ and $y =$		DM1 A1, A1 [6]	M1 for attempt to solve quadratic A1 for each 'pair'			
Or , using v	ector approach:					
$\overrightarrow{AB} = \begin{pmatrix} 4\\2 \end{pmatrix}$		B1	May be implied			
$\overrightarrow{OC} = \begin{pmatrix} 1\\4 \end{pmatrix} + \begin{pmatrix} -2\\4 \end{pmatrix} = \begin{pmatrix} -1\\8 \end{pmatrix}$		M1 A1, A1	M1 for correct approach A1 for each element correct			
$\overrightarrow{OC} = \begin{pmatrix} 1 \\ 4 \end{pmatrix} +$	$-\begin{pmatrix}2\\-4\end{pmatrix} = \begin{pmatrix}3\\0\end{pmatrix}$	A1,A1	A1 for	each element corre	ect	

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11 (a) (i) $\begin{pmatrix} 4\\4 \end{pmatrix}$	$\begin{pmatrix} 3\\3 \end{pmatrix}$	B1 [1]		
(ii) A ²	$e^{2} = \begin{pmatrix} 16 & 9\\ 12 & 13 \end{pmatrix}$	B1, B1 [2]	B1 for any 2 correct elem B1 for all correct	ents
	s the inverse matrix of \mathbf{A}^2 $\frac{1}{100} \begin{pmatrix} 13 & -9 \\ -12 & 16 \end{pmatrix}$	√B1, √B1 [2]	Follow through on their A	2
(b) det $C = x_1 = 2$.	$(x-1) - (-1)(x^2 - x + 1)$ $x^2 - 2x + 1$	M1 A1	M1 for attempt to obtain of A1 for this correct quadra from a correct det C	
$b^2 - 4ac <$	< 0, 4 – 8 < 0	DM1	DM1 for use of discrimin- solve using the formula, c complete the square in ord are no real roots.	or attempt to
No real so	blutions (so det $\mathbf{C} \neq 0$)	A1 [4]	A1 for correct reasoning of there are no real roots.	or statement that

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12	(a)	(i)	Min point a	9, $f(8) = 191$ t (0, -1) or when $y = -1$ $1 \le y \le 299$	M1 B1 A1		M1 for substitution of either $x = -10$ or x = 8, may be seen on diagram B1 May be implied from final answer, may be seen on diagram Must have \leq for A1, do not allow x Allow any domain which will make f a one-one function Assume upper and lower bound when necessary. M1 for complete method to find the form inverse function, must involve ln or lg if appropriate. May still be in terms of y. A1 must be in terms of x				
		(ii)	$x \ge 0$ or equ		B1	[3] [1]					
	(b)	(i)	$g^{-1}(x) = \ln \left(\frac{1}{4}\right)$ or $\frac{\lg\left(\frac{x+1}{4}\right)}{\lg\left(\frac{x+1}{4}\right)}$		M1 A1	[2]					
		(ii)	$gh(x) = g(1)$ $= 4e^{11}$ $20x - 2 = 1$		M1 A1 A1	[3]	A1 for	correct order correct expression correct solution fr			
			Or $h(x) = g$ 1n5x = 1 leading to x	n5	M1 A1 A1		M1 for correct order A1 for correct equation A1 for correct solution from correct working				